Short-range constraints on chemical and structural variations in bavenite

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ABSTRACT

Bavenite is an orthorhombic calcium beryllium aluminosilicate, $a \approx 23.2$, $b \approx 5.0$, $c \approx 19.4$ Å, $V \approx$ 2250 Å³, Z = 4, that crystallizes in the space group Cmcm. The crystal structures of 24 bavenite samples from various localities worldwide were refined to R_1 values from 2.4 to 7.5% based on ~1330 unique reflections collected with Mo-Ka X-radiation on a Bruker P4 CCD single-crystal diffractometer. The composition of each crystal was determined by electron microprobe analysis. There is extensive solid-solution in bavenite according to $^{O(2)}OH^- + {}^{T(4)}Si^{4+} + {}^{T(3)}Be^{2+} \rightleftharpoons {}^{O(2)}O^{2-} + {}^{T(4)}Al^{3+} + {}^{T(3)}Si^{4+}$, such that the general formula may be written $Ca_4Be_xSi_9Al_{4-x}O_{28-x}(OH)_x$, where x ranges from 2.00 to ~3.00 a.p.f.u. Small amounts of additional Be may be incorporated into bavenite *via* the substitution $^{T(3)}$ Be + $^{O(2)}$ OH⁻ + Na + $^{T(4)}$ Si₂ \rightleftharpoons $^{T(3)}$ Si + $^{O(2)}$ O²⁻ + Ca + $^{T(4)}$ Al₂. Local (short-range) bond-valence considerations indicate that Short-Range Order (SRO) should be extensive in the bavenite structure, and this is confirmed by Fourier Transform Infrared (FTIR) spectroscopy in the principal OH-stretching region and by ²⁷Al Magic Angle Spinning Nuclear Magnetic Resonance (MAS NMR) spectroscopy. Short-range bond-valence considerations indicate that the T(3)-T(4)-T(3)-T(4) rings of the framework can incorporate any short-range arrangement of cations consonant with their site populations [T(3) =Be,Si; T(4) = Si,Al], and ²⁷Al MAS NMR spectroscopy confirms this, showing the presence of the local clusters $T^{(3)}Be^{-T(4)}Al^{-T(3)}Be$, $T^{(3)}Si^{-T(4)}Al^{-T(3)}Be$ and $T^{(3)}Si^{-T(4)}Al^{-T(3)}Si$. Incorporation of Be at the T(3) site is accompanied by local replacement of O^{2-} by (OH)⁻ at the O(2) site and hydrogen bonding to the adjacent O(3) anion; the latter promotes Be \rightarrow Si substitution at the T(3) tetrahedron adjacent in the **b** direction. T(3)-T(4)-T(3)-T(4) rings link in the **c** direction through a T(3)-(1)-(3)linkage [T(1) = Si]. Local bond-valence considerations show that occupancy of both T(3) tetrahedra by Be violates the valence-sum rule, and that the linkage $T^{(3)}Be^{-T^{(1)}}Si^{-T^{(3)}}Si$ provides the constraint whereby Be does not exceed 3 a.p.f.u. in bavenite when incorporated *via* the substitution $^{O(2)}OH^- + ^{T(4)}Si^{4+} + ^{T(3)}Be^{2+} \rightleftharpoons ^{O(2)}O^{2-} + ^{T(4)}Al^{3+} + ^{T(3)}Si^{4+}$.

Keywords: Bavenite, crystal-structure refinement, IR, ²⁷Al MAS NMR, EMPA, beryllium, end-members, solid-solution.

Introduction

BAVENITE is a calcium beryllium aluminosilicate mineral occurring primarily in granitic pegmatites (Černý, 2002). It is a widespread product of

* E-mail: frank_hawthorne@umanitoba.ca DOI: 10.1180/minmag.2011.075.1.213 hydrothermal alteration, particularly of beryl (Černý, 1968; Bondi *et al.*, 1983), and can occur as pseudomorphs after beryl. It also occurs as coatings on feldspar and quartz in miarolitic pegmatites (Tennyson, 1960; Janeczek, 1985). Bavenite has been reported from pneumatolytically altered syenites (Petersen *et al.*, 1995), where it is definitely not pseudomorphic, occurring as large (up to 1.5 cm) freestanding crystals on albite. The first detailed chemical compositions were given by Switzer and Reichen (1960), Berry (1963), Beus (1966) and Cannillo *et al.* (1966), and both Cannillo *et al.* (1966) and Kharitonov *et al.* (1971) showed that the crystal structure is a framework of silicate and beryllate tetrahedra with the formula Ca₄ [Be_(2+x)Al_(2-x)] [Si₉O_(26-x)(OH)_(2+x)]. Different substitution mechanisms have been proposed to account for the variation in chemical composition of bavenite. Berry (1963) suggested direct Be \Rightarrow Al with electroneutrality maintained by the incorporation of H. Cannillo *et al.* (1966) solved the structure of bavenite; they assigned Be and Al to the *T*(2) and *T*(4) tetrahedra, and proposed that additional minor Be replaces Al at the *T*(4) site. In addition, IR spectra were reported by Petersen *et al.* (1995).

In the present study, we have characterized the crystal structure and crystal chemistry of 24 samples of bavenite (Table 1) using single-

crystal X-ray diffraction (XRD), IR spectroscopy and electron microprobe analysis (EMPA) in order to examine the details of the substitution mechanism, the role of hydrogen bonding in the structure, and the character of short-range order associated with the solid solution. Several other samples were also characterized by crystalstructure refinement and EMPA, and show disorder that is not present in the samples described here; these results will be reported at a later date.

Experimental

X-ray diffraction

Crystals were selected for study based on optical clarity and uniform extinction in cross-polarized light. Each fragment was attached to the end of a

| T 1 | 1 | T' 4 | C | 1 . | 1 | 1 | 1 | C | |
|---------|-----|-------|-----|----------|---------|-----|------------|----|---------|
| LARIE | | L 1ST | OT. | pavenite | samples | and | locations | OT | origin |
| INDLL . | · · | LIDU | 01 | ouvenite | Sumpres | unu | iocutionio | 01 | origin. |

| | Locality | Other number | Source |
|-------|--|--------------|--------|
| 2ABAV | Rincon, San Diego County, California | 118245-B | b |
| 7BAV | Ilimaussaq, Kangerluarsuk Fjord, Greenland | 134693 | b |
| 10BAV | Government Pit, Albany, New Hampshire | 119542 | b |
| 11BAV | Kalisay, Kyrgizstan | _ | а |
| 12BAV | Baveno, Italy | E3365 | с |
| 13BAV | Londonderry, West Australia | M23357 | с |
| 14BAV | Sandvik Property, Zealand Twp., Kenora District, | M405225 | с |
| 15BAV | Foote Mine, King's Mountain, Cleavland County, North Carolina | teach113 | с |
| 19BAV | Lily Pad Lake, Fort Hope, Ontario, Canada | M38292 | с |
| 21BAV | Aple Rossa, Oresco, Novara, Italy | M41009 | с |
| 23BAV | Oresco, Val Vigeddo, Italy | _ | d |
| 25BAV | Ascham Alm, Untersulzbachtal, Salzburg, Austria | _ | е |
| 27BAV | Lily Pad Lake, Fort Hope, Ontario, Canada | M6128 | f |
| 28BAV | Lily Pad Lake, Fort Hope, Ontario, Canada | M5617 | f |
| 29BAV | Lily Pad Lake, Fort Hope, Ontario, Canada | M5617 | f |
| 31BAV | Drahonin A, Czech Republic | a 122 | g |
| 32BAV | Marsikov, Schinderhubel 1, Czech Republic | a 1380 | g |
| 33BAV | Vlastejovice, Czech Republic | B 5963 | g |
| 35BAV | Mont Saint-Hilaire, Quebec, Canada | _ | j |
| 36BAV | Nye Rull, Buskerud, Norway | _ | i |
| 37BAV | Baveno, Italy | _ | i |
| 39BAV | Norway | _ | i |
| 40BAV | Lily Pad Lake, Fort Hope, Ontario, Canada | _ | k |
| 41BAV | Ekaterinburg (near), Ural, Russia | _ | k |

a: Excaliber Mineral Co.; b: Harvard University; c: Royal Ontario Museum;

d: Dealer; e: Natural History Museum, Vienna; f: Petr Černý;

g: Moravia Museum of Mineralogy; h: Geologisk Museum, Copenhagen;

i: Roy Kristiansen; j: Andy McDonald; k: Chris Pedersen.

tapered glass fibre and mounted on a Bruker P4 automated four-circle X-ray diffractometer equipped with a graphite monochromated Mo-Ka X-radiation and a Bruker 4K CCD detector. X-ray intensity data were collected to $60^{\circ}2\theta$ with a frame width of 0.2° and frame times from 40 to 120 s to ensure equal data coverage for crystals of different size. Unit-cell dimensions were derived for each crystal by least-squares refinement of ~1720 unique reflections in the Ewald sphere; values are given in Table 2, together with other information relevant to data collection and structure refinement. The data were corrected for absorption, Lorentz, polarization and background effects, averaged and reduced to structure factors.

Chemical composition

Crystals were analysed using a Cameca SX-100 electron microprobe operating in wavelengthdispersion mode with an accelerating voltage of 15 kV, a specimen current of 15 nA, and a beam diameter of 10 μ m. The following standards were used: TAP: Al, andalusite; Si, diopside; LTAP: Mg, olivine; LLiF: Mn, spessartine; Fe, fayalite; Na, albite; LPET: K, orthoclase; Ca, diopside. Unit formulae were normalized on the basis of 28 anions with Be = 13 - (Si + Al) a.p.f.u. (atoms per formula unit) and OH was iterated until (Ca + Na) = (Al + Be). Chemical compositions (mean of 10 determinations) and unit formulae are given in Table 3.

Crystal-structure refinement

The structure of each sample was refined in the space group Cmcm using F^2 in the SHELXTL PLUS (PC version) software package; initial positional parameters were those of Cannillo et al. (1966). Full occupancy was assumed for all sites, and there was no subsequent indication of vacancies. The T(3) site is occupied by Si and Be, and the site occupancies were allowed to vary during refinement, subject to the constraint that Si + Be = 1. The position of the H atom associated with the O(8) O atom was taken from difference-Fourier maps and refined with a fixed isotropicdisplacement parameter and fixed occupancy. The constraint of electroneutrality indicates that some crystals have H present in addition to that attached to O(8). Bond-valence calculations showed that this additional H is attached to the O atom at the O(2) site, but the exact position of this H could not be seen on difference-Fourier maps, perhaps because of local disorder associated with variations in short-range bond-valence values (see later discussion). An extinction correction was introduced in the final stages of refinement, and all structures converged to R_1 indices in the range 2.3-7.5%, although the majority (20 structures) are in the range 2.3-4.5%. Final atom coordinates and isotropic-displacement parameters are given in Table 4; anisotropic-displacement parameters for all structures have been deposited with the editor of the journal and are available at http:// www.minersoc.org/pages/e journals/ dep mat mm.html. Selected interatomic distances are given in Table 5, refined site-scattering values (Hawthorne et al., 1995) are given in Table 6 (where they are compared with the values from the unit formulae derived from chemical compositions determined by EMPA), and Table 7 shows selected bond-valence tables calculated with the parameters of Brown and Altermatt (1985).

Fourier-transform infrared spectroscopy (FTIR)

A Bruker Tensor 27 Fourier-transform infrared (FTIR) spectrometer equipped with an MCT detector was used to collect spectra on five powdered samples of bavenite (25BAV, 32BAV, 35BAV, 40BAV and 41BAV). For 25BAV and 35BAV, we collected X-ray powder patterns to check for impurity phases, but none was found; there was insufficient material to do so for the other samples. Approximately 5 mg of ground mineral was combined with 145 mg of ground KBr and pressed into a single pellet under 10 tons of pressure for 20-30 min. All pellets were thoroughly dried in a heated desiccator at ~106°C for 8-10 h to ensure minimal adsorption of water. For each spectrum, a total of 1000 scans was collected between 4000 and 600 \mbox{cm}^{-1} at a resolution of 4 cm^{-1} and a beam size of 6 mm. Spectra were analysed by fitting symmetric-Gaussian peaks and an asymmetric-Gaussian background with the software package PeakFit[®] (v.4) by optimization and least-squares refinement until an acceptable fit to the spectral shape was obtained.

Magic-Angle-Spinning Nuclear Magnetic Resonance (MAS NMR) spectroscopy

A Varian Inova 600 spectrometer (14.1 T) was used to record MAS NMR spectra of ^{27}Al (v_L = 156.3 MHz) for 40BAV and 41BAV. For each

| | 2ABAV | 7BAV | 10BAV | 11BAV | 12BAV | 13BAV | 14BAV | 15BAV |
|---------------------------------|----------------------------|----------------------------|---------------------------|----------------------------|----------------------------|----------------------------|---------------------------|----------------------------|
| a (Å) | 23.2080(10) | 23.2028(6) | 23.2068(14) | 23.2110(10) | 23.198(2) | 23.2164(10) | 23.2066(9) | 23.1995(11) |
| b (\mathbf{A}) | 4.9833(2) | 4.9805(1) | 4.9929(3) | 4.9721(2) | 4.9620(4) | 5.0023(2) | 4.9681(2) | 5.0111(2) |
| c (Å) | 19.4266(8) | 19.4290(5) | 19.4340(12) | 19.4189(7) | 19.4262(14) | 19.4447(7) | 19.4085(8) | 19.4454(9) |
| $V(Å^3)$ | 2246.7(3) | 2245.2(2) | 2251.7(4) | 2241.1(3) | 2236.1(5) | 2258.2(3) | 2237.7(3) | 2260.6(3) |
| R_1 | 2.95 | 2.33 | 3.34 | 2.77 | 4.50 | 3.10° | 3.03 | 2.92 |
| wR_2 | 8.14 | 6.83 | 8.41 | 7.54 | 9.78 | 8.66 | 8.11 | 7.28 |
| GoF | 1.036 | 1.074 | 1.032 | 1.077 | 0.890 | 1.093 | 1.002 | 1.001 |
| Reflections collected | 10670 | 10610 | 10761 | 10706 | 10649 | 10741 | 10524 | 10733 |
| Reflections merged | 1709 | 1713 | 1726 | 1708 | 1709 | 1726 | 1709 | 1732 |
| $\Sigma F_{ m O} > 4\sigma F$ | 1306 | 1491 | 1291 | 1358 | 968 | 1497 | 1315 | 1277 |
| Rint ORTH | 4.9 | 3.0 | 6.0 | 3.9 | 13.8 | 3.4 | 5.0 | 5.8 |
| Crystal dimensions (µm) | $50 \times 50 \times 240$ | $80 \times 100 \times 120$ | $140 \times 200x$ 3 | $180 \times 100 \times 40$ | $100 \times 200 \times 2$ | $120 \times 240 \times 30$ | $60 \times 160 \times 25$ | $120 \times 200 \times 10$ |
| | 19BAV | 21BAV | 23BAV | 25BAV | 27BAV | 28BAV | 29BAV | 31BAV |
| <i>a</i> (Å) | 23.2075(8) | 23.2077(12) | 23.197(3) | 23.2120(7) | 23.2090(7) | 23.2074(7) | 23.2066(7) | 23.2096(14) |
| b $(Å)$ | 5.0063(2) | 5.0096(2) | 4.9847(5) | 5.0043(1) | 5.0129(1) | 5.0098(2) | 4.9960(2) | 5.0020(3) |
| c (Å) | 19.4428(7) | 19.4422(8) | 19.416(2) | 19.4439(6) | 19.4494(6) | 19.4477(7) | 19.4373(7) | 19.4386(10) |
| $V(Å^3)$ | 2258.9(2) | 2260.4(3) | 2245.2(7) | 2258.6(2) | 2262.8(2) | 2261.1(2) | 2253.6(2) | 2256.7(4) |
| R_1 | 2.52 | 3.02 | 5.72 | 2.51 | 2.35 | 2.49 | 2.34 | 3.60 |
| wR_2 | 7.29 | 7.08 | 10.81 | 7.12 | 7.02 | 6.71 | 7.01 | 9.02 |
| GoF | 1.123 | 0.960 | 0.889 | 1.101 | 1.062 | 1.052 | 1.130 | 1.047 |
| Reflections collected | 10619 | 10780 | 10625 | 10750 | 10705 | 10754 | 10702 | 10664 |
| Reflections merged | 1729 | 1726 | 1708 | 1727 | 1724 | 1731 | 1724 | 1721 |
| $\Sigma F_{ m O} > 4\sigma F$ | 1428 | 1235 | 856 | 1516 | 1494 | 1366 | 1433 | 1353 |
| $R_{ m int}$ orth | 4.0 | 6.5 | 20.1 | 3.0 | 3.2 | 4.3 | 3.2 | 5.6 |
| Crystal dimensions (µm) | $60 \times 100 \times 160$ | $110 \times 130 \times 16$ | $140 \times 25 \times 13$ | $80 \times 80 \times 180$ | $70 \times 140 \times 160$ | $80 \times 80 \times 100$ | $80 \times 80 \times 200$ | $100 \times 140 \times 20$ |

TABLE 2. Data collection and structure-refinement information for bavenite samples.

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| sample, weighed amounts (10-35 mg) of |
|---|
| powdered sample (~15 μm crystallites) were |
| placed in a 3.2 mm (22 μL capacity) zirconia |
| rotor and spun at a speed of 18 kHz (41BAV) and |
| 22 kHz (40BAV) in a double-resonance probe. An |
| optimized recycle delay of 60 s was used for both |
| samples, as this was determined to be more than |
| sufficient to ensure complete relaxation. The final |
| spectra are composites of 1024 averaged scans. |
| Spectra are referenced to $1.1 M \text{ Al}(\text{NO}_3)_3$. Pulse |
| widths were selected to coincide approximately |
| with a 20° tip angle at an rf nutation frequency of |
| 50 kHz. The ²⁷ Al spectra for bavenite lack well |
| defined lineshapes required to obtain NMR |
| parameters by simulation. For both spectra, |
| component peaks were sufficiently resolved to |
| allow reliable modelling using symmetric |
| Lorentzian-Gaussian peakshapes, from which the |
| integrated intensities for each peak could be |
| determined. |

General structure description

Bavenite has a framework structure of silicate and beryllate tetrahedra (Cannillo *et al.*, 1966). Fourmembered rings of alternating SiO₄ and AlO₄ tetrahedra link through six-membered rings of SiO₄ tetrahedra to form chains that extend in the **a** direction (Fig. 1*a*). Adjacent chains link through linear BeO₄–SiO₄–BeO₄ groups, forming two types of six-membered rings between the chains: $[^{T(2)}Be - ^{T(1)}Si - ^{T(3)}(Si,Be) - ^{T(4)}(A1,Si) - ^{T(5)}Si - ^{T(6)}Si]$ and $[^{T(2)}Be - ^{T(6)}Si - ^{T(6)}Si - ^{T(2)}Be - ^{T(6)}Si - ^{T(6)}Si]$ (Fig. 1*b*). These sheets stack in the **b** direction (Fig. 2), with AlO₄ tetrahedra as the linking elements between the sheets. This arrangement results in large cavities that contain the [7]-coordinated interstitial Ca.

In the bayenite structure, the ratio of the number of tetrahedral cations and anions is 13:28, indicating that the framework is interrupted (i.e. all anions do not link to two T cations). For a completely continuous framework structure, the ideal formula is $[T\Phi_2]_n$ where Φ is an unspecified anion. A completely connected framework of tetrahedra with thirteen cations would have the formula $[T_{13}\Phi_{26}]$, and hence the formula $[T_{13}\Phi_{28}]$ must have four [1]-coordinated anions. These are the O(2) and O(8) anions, both of which occur twice in the formula unit $[T_{13}\Phi_{28}]$. Bond-valence considerations (see below) show that O(8) is always an (OH) group, and O(2) may be O or (OH), depending on the details of the short-range coordination.

| | 32BAV | 33BAV | 35BAV | 36ABAV | 37BAV | 39BAV | 40BAV | 41BAV |
|---|---------------------------|----------------------------|---------------------------|----------------------------|---------------------------|----------------------------|--------------------------|---------------------------|
| $\begin{array}{c} a & (\mathring{A}) \\ b & (\mathring{A}) \end{array}$ | 23.1995(12) 4.9743(3) | 23.1949(11) 5.0067(2) | 23.251(2) 4.9734(5) | 23.2043(11) 5.0005(5) | 23.2272(6) 5.0028(1) | 23.2051(11) 4.9986(2) | 23.1895(12) 4.9725(2) | 23.1961(13) 4.9937(3) |
| $\begin{array}{c} c \left(\dot{A} \right) \\ c \left(\dot{A} \right) \\ V \left(\dot{A} \right) \end{array}$ | 19.4255(9) | 19.4370(8) | 19.4678(14) | 19.4426(9) | 19.4518(5) | 19.4375(9) | 19.4488(9) | 19.4296(11) |
| R_1 | 3.43 | 3.06 | 7.28 | 5.08 | 3.22 | 3.22 | 3.74 | 7.45 |
| wR ₂ | 8.46 | 8.33 | 16.21 | 10.04 | 7.52 | 7.98 | 8.95 | 13.76 |
| GoF | 1.071 | 1.028 | 1.024 | 1.316 | 1.157 | 1.082 | 1.127 | 1.404 |
| ΣReflections collected | 10626 | 10694 | 10583 | 11092 | 10565 | 10525 | 10945 | 10976 |
| ΣReflections merged | 1710 | 1724 | 1714 | 1719 | 1719 | 1719 | 1715 | 1725 |
| $\Sigma F_{0} > 4\sigma F$ | 1367 | 1399 | 1082 | 1729 | 1447 | 1338 | 1649 | 1715 |
| $R_{ m int}$ or th | 5.6 | 4.4 | 16.6 | 2.9 | 3.9 | 5.0 | 2.9 | 3.5 |
| Crystal dimensions (µm) | $40 \times 80 \times 140$ | $30 \times 130 \times 220$ | $100 \times 100 \times 4$ | $100 \times 160 \times 40$ | $140 \times 80 \times 38$ | $100 \times 180 \times 15$ | $20 \times 50 \times 50$ | $60 \times 60 \times 150$ |

Table 2 (contd.)

Results

Site populations

Crystal-structure refinement indicates that variation in site-scattering values occurs only at the T(3) site (Table 6). In addition, there is significant variation in $\langle T-O \rangle$ bondlengths at the T(3) and T(4) sites. The $\langle T-O \rangle$ bondlengths at T(1), T(2), T(5) and T(6) show little variation: $\langle T(1)-O \rangle =$ 1.636(2), $\langle T(2)-O \rangle =$ 1.646(2), $\langle T(5)-O \rangle =$ 1.620(4), $\langle T(6)-O \rangle =$ 1.618(1) Å. The variation in $\langle T(1)-O \rangle$, $\langle T(5)-O \rangle$ and $\langle T(6)-O \rangle$, 1.618-1.636 Å, is in accord with the variation in mean anion coordination number ([4], [2.5] and [2.25], respectively) for SiO₄ tetrahedra (Brown and Gibbs, 1969), and hence we assign T(1) =T(5) = T(6) = Si. Site-scattering indicates that T(2)is occupied by Be, as found by Cannillo *et al.* (1966). The < T(2)–O> distance of 1.646(2) Å is somewhat longer than the grand <Be–O> distance in minerals of 1.633 Å reported by Hawthorne and Huminicki (2002), but still lies well within the dispersion of their data, and the low scatter in bavenite indicates that T(2) is completely occupied by Be as proposed by Cannillo *et al.* (1966). Thus, the principal variation at the *T* sites involves (1) variation in site scattering at T(3), and (2) variation in < T–O> at T(4).

Variation in site scattering at T(3) is accompanied by little or no change in the $\langle T(3)-O \rangle$ bondlength (~1.625 Å), which is in accord with occupancy of T(3) by Be and Si (with radii of 0.27 and 0.26 Å, respectively, Shannon, 1976). Figure 3 shows the variation in Be calculated from the chemical compositions of the crystals

TABLE 3. EMPA-derived composition of single crystals.

| | | 2ABAV | 7BAV | 10BAV | 11BAV | 12BAV | 13BAV | 14BAV | 15BAV | 19BAV | 21BAV | 23BAV | 25BAV |
|--------------------------------|----------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| Na ₂ O | | 0.17 | 0.08 | 0.13 | 0.02 | 0.30 | 0.12 | 0.09 | 0.03 | 0.0 | 0.01 | 0.04 | 0.05 |
| Al ₂ O ₃ | ; | 6.57 | 8.23 | 7.74 | 5.87 | 3.54 | 8.23 | 5.17 | 10.30 | 9.5 | 9.99 | 7.30 | 9.60 |
| SiO_2 | | 59.15 | 59.35 | 59.41 | 58.82 | 61.48 | 58.34 | 59.37 | 57.67 | 59.0 | 58.13 | 59.03 | 58.22 |
| CaO | | 24.14 | 23.95 | 24.26 | 24.79 | 23.44 | 23.89 | 24.49 | 24.39 | 24.3 | 24.41 | 24.51 | 24.25 |
| BaO | | 7.68 | 6.71 | 7.12 | 8.19 | 8.96 | 6.71 | 8.46 | 5.85 | 6.2 | 5.99 | 7.38 | 6.15 |
| H_2O | | 2.83 | 2.50 | 2.62 | 2.91 | 3.48 | 2.46 | 3.07 | 2.06 | 2.2 | 2.13 | 2.66 | 2.21 |
| Total | | 100.54 | 100.82 | 101.28 | 100.60 | 101.20 | 99.76 | 100.64 | 100.29 | 101.3 | 100.66 | 100.92 | 100.47 |
| Ca: | Na | 0.050 | 0.024 | 0.037 | 0.006 | 0.087 | 0.036 | 0.026 | 0.009 | 0.003 | 0.003 | 0.012 | 0.015 |
| | Ca | 3.940 | 3.917 | 3.946 | 4.042 | 3.745 | 3.953 | 3.977 | 4.050 | 3.976 | 4.033 | 3.999 | 4.007 |
| | Σ | 3.990 | 3.941 | 3.983 | 4.048 | 3.832 | 3.989 | 4.003 | 4.060 | 3.979 | 4.036 | 4.011 | 4.022 |
| <i>T</i> (1): | Si | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| T(2) | Be | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| <i>T</i> (3) | Si | 1.189 | 1.540 | 1.402 | 1.005 | 0.790 | 1.510 | 0.920 | 1.822 | 1.740 | 1.780 | 1.299 | 1.723 |
| | Be | 0.811 | 0.460 | 0.598 | 0.995 | 1.210 | 0.490 | 1.080 | 0.178 | 0.260 | 0.220 | 0.701 | 0.277 |
| | Σ | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| T(2) | Si | 0.821 | 0.519 | 0.615 | 0.947 | 1.378 | 0.501 | 1.077 | 0.118 | 0.282 | 0.184 | 0.690 | 0.255 |
| | Al | 1.179 | 1.481 | 1.385 | 1.053 | 0.622 | 1.499 | 0.923 | 1.882 | 1.718 | 1.816 | 1.310 | 1.745 |
| | Σ | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| T(5) | Si | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| T(6) | Si | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 |
| O(1)- | -O(7): O | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 |
| O(8): | OH | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| O(2): | 0 | 1.129 | 1.457 | 1.348 | 1.047 | 0.535 | 1.463 | 0.897 | 1.872 | 1.715 | 1.813 | 1.298 | 1.730 |
| | OH | 0.871 | 0.543 | 0.652 | 0.953 | 1.465 | 0.537 | 1.103 | 0.128 | 0.285 | 0.187 | 0.702 | 0.270 |
| | Σ | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |

determined by EMPA (Table 3) as a function of the Be content of the T(3) site determined by SREF (Hawthorne and Grice, 1990). The data scatter about the 1:1 line, but there is a tendency to lie slightly below the 1:1 line; however, using ionized scattering factors moves the data to slightly above the line. The general accord between the SREF and EMPA results indicates that both methods of deriving the Be content are reasonably accurate, and that variable Be occurs only at the T(3) site. There is no significant variation in scattering at the T(4) site and yet there is significant variation in the < T(4) - O > distances (Table 5) from 1.653–1.730 Å. This variation in < T(4) - O > and lack of variation in site scattering is compatible with occupancy of T(4) by Si (Z = 14, r = 0.26 Å) and Al (Z = 13, r = 0.39 Å). In accord with this conclusion, there is a linear

Table 3 (contd.)

relation between < T(4) - O > and the Al content of the crystal (Fig. 4). Figure 5 shows the variation of Al at the T(4) site as a function of Be at the T(3) site. This inverse 1:1 relation is in exact accord with the substitution

Hydrogen bonding

Inspection of the bond-valence tables (Table 7) for crystals 14BAV (high Be) and 27BAV (low Be) shows that, omitting hydrogen bonds, two anions have incident bond-valence sums significantly less than the value of 2 v.u. (valence units) expected from the valence-sum rule (Brown,

| | | 27BAV | 28BAV | 29BAV | 31BAV | 32BAV | 33BAV | 35BAV | 36ABAV | 37BAV | 39BAV | 40BAV | 41BAV |
|-------------------|---------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| Na ₂ O | | 0.04 | 0.02 | 0.03 | 0.07 | 0.05 | 0.03 | 0.50 | 0.06 | 0.09 | 0.06 | 0.10 | 0.05 |
| Al_2O_3 | | 9.79 | 10.32 | 6.12 | 8.83 | 6.19 | 9.08 | 3.36 | 9.19 | 7.78 | 7.50 | 5.65 | 8.19 |
| SiO ₂ | | 58.10 | 58.54 | 59.45 | 58.47 | 59.42 | 57.69 | 60.80 | 58.97 | 58.85 | 58.81 | 59.03 | 57.88 |
| CaO | | 23.43 | 24.39 | 24.38 | 24.33 | 24.48 | 24.16 | 23.84 | 24.01 | 24.10 | 24.44 | 23.97 | 23.95 |
| BaO | | 5.68 | 5.83 | 7.90 | 6.58 | 7.92 | 6.35 | 9.39 | 6.25 | 7.00 | 7.27 | 8.00 | 6.70 |
| H_2O | | 2.12 | 2.09 | 2.88 | 2.37 | 2.88 | 2.26 | 3.58 | 2.31 | 2.57 | 2.62 | 2.95 | 2.43 |
| Total | | 99.16 | 101.19 | 100.75 | 100.64 | 100.93 | 99.57 | 101.47 | 100.78 | 100.39 | 100.70 | 99.70 | 99.20 |
| Ca: | Na | 0.012 | 0.006 | 0.009 | 0.022 | 0.014 | 0.010 | 0.145 | 0.018 | 0.027 | 0.018 | 0.030 | 0.015 |
| | Ca | 3.919 | 4.010 | 3.966 | 4.002 | 3.977 | 4.024 | 3.803 | 3.943 | 3.956 | 4.000 | 3.932 | 3.989 |
| | Σ | 3.931 | 4.016 | 3.975 | 4.024 | 3.990 | 4.034 | 3.948 | 3.961 | 3.983 | 4.018 | 3.962 | 4.004 |
| <i>T</i> (1) | Si | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| T(2) | Be | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| <i>T</i> (3) | Si | 1.870 | 1.850 | 1.120 | 1.573 | 1.115 | 1.630 | 0.642 | 1.699 | 1.422 | 1.333 | 1.058 | 1.497 |
| | Be | 0.130 | 0.150 | 0.880 | 0.427 | 0.885 | 0.370 | 1.358 | 0.301 | 0.578 | 0.667 | 0.942 | 0.503 |
| | Σ | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| T(2) | Si | 0.199 | 0.133 | 0.905 | 0.403 | 0.895 | 0.336 | 1.410 | 0.340 | 0.595 | 0.649 | 0.980 | 0.500 |
| | Al | 1.801 | 1.867 | 1.095 | 1.597 | 1.105 | 1.664 | 0.590 | 1.660 | 1.405 | 1.351 | 1.020 | 1.500 |
| | Σ | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| <i>T</i> (5) | Si | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| <i>T</i> (6) | Si | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 | 4.000 |
| O(1)-C | D(7): O | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 | 24.000 |
| O(8): | OH | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| O(2): | 0 | 1.789 | 1.861 | 1.086 | 1.575 | 1.092 | 1.654 | 0.445 | 1.642 | 1.378 | 1.333 | 0.990 | 1.485 |
| | OH | 0.211 | 0.139 | 0.914 | 0.425 | 0.908 | 0.346 | 1.555 | 0.358 | 0.622 | 0.667 | 1.010 | 0.515 |
| | Σ | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 |
| | | | | | | | | | | | | | |

| | | 2ABAV | 7BAV | 10BAV | 11BAV | 12BAV | 13BAV | 14BAV | 15BAV |
|--------------|--------------------------------|--|--|--|--|--|--|--|--|
| Ca | x | 0.08316(2) | 0.08264(1) | 0.08343(2) | 0.08246(2) | 0.08175(4) | 0.08358(2) | 0.08246(2) | 0.08409(2) |
| | y | 0.25083(10) | 0.25225(7) | 0.24779(10) | 0.25168(9) | 0.2578(2) | 0.24639(8) | 0.25474(10) | 0.24341(9) |
| | z | 0.15316(3) | 0.15336(2) | 0.15288(3) | 0.15327(2) | 0.15418(4) | 0.15279(2) | 0.15347(2) | 0.15245(3) |
| | U _{eq} | 0.01349(13) | 0.01283(10) | 0.01301(14) | 0.01355(12) | 0.0142(2) | 0.01325(13) | 0.01302(13) | 0.01013(12) |
| <i>T</i> (1) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.7762(3) | 0.77468(17) | 0.7773(3) | 0.772(2) | 0.7725(5) | 0.7774(2) | 0.7742(3) | 0.7795(3) |
| | z | $\frac{1}{4}$ | ¹ ⁄ ₄ | ¹ / ₄ | ¹ ⁄ ₄ | ¹ / ₄ | ¹ / ₄ | ¹ / ₄ | ¹ ⁄ ₄ |
| | U _{eq} | 0.0086(3) | 0.00850(17) | 0.0088(3) | 0.0095(2) | 0.0081(5) | 0.0093(2) | 0.0079(3) | 0.0067(3) |
| <i>T</i> (2) | x | 0.12460(18) | 0.12434(13) | 0.1248(2) | 0.12424(17) | 0.1241(3) | 0.12475(16) | 0.12439(18) | 0.1249(2) |
| | y | 0.8188(9) | 0.8213(6) | 0.8179(9) | 0.8211(8) | 0.8235(16) | 0.8158(8) | 0.8223(9) | 0.8140(9) |
| | z | ¹ / ₄ | ¹ / ₄ | ¹ / ₄ | ¹ ⁄ ₄ | ¹ / ₄ | ¹ / ₄ | ¹ / ₄ | ¹ ⁄ ₄ |
| | U _{eq} | 0.0074(8) | 0.0106(5) | 0.0092(9) | 0.0118(8) | 0.0100(17) | 0.0097(7) | 0.0092(8) | 0.0091(9) |
| <i>T</i> (3) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.7224(3) | 0.72113(18) | 0.7228(2) | 0.7203(3) | 0.7216(6) | 0.72300(19) | 0.7220(3) | 0.72322(19) |
| | z | 0.10362(7) | 0.10437(5) | 0.10419(7) | 0.10458(6) | 0.10338(14) | 0.10435(5) | 0.10354(8) | 0.10442(5) |
| | U _{eq} | 0.0083(4) | 0.0087(3) | 0.0080(4) | 0.0094(4) | 0.0084(9) | 0.0098(3) | 0.0087(5) | 0.0066(3) |
| <i>T</i> (4) | x y z U _{eq} | 0.09415(4) ^{1/2} 0 0.0065(3) | 0.09400(3) ^{1/2} 0 0.0071(2) | 0.09465(5) ^{1/2} 0 0.0078(3) | $\begin{array}{c} 0.09372(4) \\ \frac{1}{2} \\ 0 \\ 0.0081(3) \end{array}$ | $\begin{array}{c} 0.09309(7) \\ \frac{1}{2} \\ 0 \\ 0.0076(5) \end{array}$ | 0.09492(4) ^{1/2} 0 0.0087(3) | 0.09334(4) ^{1/2} 0 0.0066(3) | $\begin{array}{c} 0.09567(4) \\ \frac{1}{2} \\ 0 \\ 0.0069(3) \end{array}$ |
| <i>T</i> (5) | x | 0.17025(4) | 0.17025(3) | 0.17020(4) | 0.17005(3) | 0.17006(7) | 0.17026(3) | 0.16995(4) | 0.17033(4) |
| | y | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | z | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | U _{eq} | 0.0099(2) | 0.00960(14) | 0.0098(2) | 0.01049(18) | 0.0089(3) | 0.01000(18) | 0.0095(2) | 0.0079(2) |
| <i>T</i> (6) | x | 0.21413(3) | 0.21395(2) | 0.21404(3) | 0.21387(2) | 0.21372(5) | 0.21409(2) | 0.21395(3) | 0.21415(3) |
| | y | 0.85950(13) | 0.86185(8) | 0.85830(14) | 0.86129(12) | 0.8670(2) | 0.85757(11) | 0.86276(13) | 0.85491(13) |
| | z | 0.14428(3) | 0.14400(2) | 0.14362(4) | 0.14392(3) | 0.14452(5) | 0.14342(3) | 0.14434(3) | 0.14311(3) |
| | U _{eq} | 0.00859(15) | 0.00858(11) | 0.00903(16) | 0.00951(13) | 0.0081(2) | 0.00931(14) | 0.00823(15) | 0.00740(15) |
| O(1) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.5757(5) | 0.5746(3) | 0.5758(5) | 0.5717(4) | 0.5756(8) | 0.5754(4) | 0.5748(5) | 0.5757(4) |
| | z | 0.18208(12) | 0.18229(8) | 0.18238(13) | 0.18225(10) | 0.18213(19) | 0.18265(10) | 0.18191(11) | 0.18288(12) |
| | U _{eq} | 0.0098(5) | 0.0099(3) | 0.0105(5) | 0.0107(4) | 0.0094(9) | 0.0105(4) | 0.0097(5) | 0.0088(5) |
| O(2) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.0366(5) | 0.0364(3) | 0.0360(5) | 0.0337(4) | 0.0370(8) | 0.0363(4) | 0.0363(5) | 0.0362(5) |
| | z | 0.11016(13) | 0.10970(9) | 0.11158(14) | 0.11071(10) | 0.1082(2) | 0.11202(12) | 0.10896(12) | 0.11344(12) |
| | U _{eq} | 0.0127(5) | 0.0129(3) | 0.0129(6) | 0.0114(4) | 0.013(1) | 0.0137(4) | 0.0112(5) | 0.0103(5) |
| O(3) | x | 0.05747(7) | 0.05766(5) | 0.05771(8) | 0.05783(6) | 0.05742(12) | 0.05767(7) | 0.05747(7) | 0.05763(7) |
| | y | 0.5972(3) | 0.5957(2) | 0.5981(4) | 0.5961(3) | 0.5933(6) | 0.5980(3) | 0.5953(4) | 0.5997(3) |
| | z | 0.06905(9) | 0.06957(6) | 0.07017(10) | 0.06979(7) | 0.06836(14) | 0.07061(8) | 0.06855(8) | 0.07143(9) |
| | U _{eq} | 0.0144(4) | 0.0147(3) | 0.0140(4) | 0.0151(3) | 0.0124(6) | 0.0151(3) | 0.0145(4) | 0.0118(4) |
| O(4) | x | 0.13055(7) | 0.13101(5) | 0.13117(8) | 0.13110(7) | 0.13069(12) | 0.13135(7) | 0.13050(7) | 0.13163(7) |
| | y | 0.2394(3) | 0.2369(2) | 0.2345(4) | 0.2367(3) | 0.2410(6) | 0.2328(3) | 0.2412(4) | 0.2302(3) |
| | z | 0.03389(10) | 0.03407(6) | 0.03488(10) | 0.03410(8) | 0.03210(13) | 0.03539(8) | 0.03336(9) | 0.03624(9) |
| | U _{eq} | 0.0143(4) | 0.0145(3) | 0.0143(4) | 0.0157(3) | 0.0141(7) | 0.0144(3) | 0.0146(4) | 0.0114(4) |

TABLE 4. Final atom positions and equivalent isotropic-displacement parameters (\AA^2) for crystals of bavenite.

CHEMICAL AND STRUCTURAL VARIATIONS IN BAVENITE

Table 4 (contd.)

| | | 2ABAV | 7BAV | 10BAV | 11BAV | 12BAV | 13BAV | 14BAV | 15BAV |
|------|-----------------|-------------------------|------------------------|---------------|---------------|---------------|-------------------------|---------------|---------------|
| O(5) | x | 0.20832(7) | 0.20826(5) | 0.20825(8) | 0.20806(6) | 0.20770(12) | 0.20829(6) | 0.20823(7) | 0.20832(7) |
| | У | 0.8702(4) | 0.8718(2) | 0.8683(4) | 0.8723(3) | 0.8777(7) | 0.8669(3) | 0.8738(4) | 0.8638(3) |
| | Z | 0.06111(9) | 0.06072(6) | 0.06049(9) | 0.06065(7) | 0.06124(13) | 0.06028(8) | 0.06105(8) | 0.05984(8) |
| | $U_{\rm eq}$ | 0.0139(4) | 0.0139(2) | 0.0140(4) | 0.0145(3) | 0.0125(6) | 0.0141(3) | 0.0134(4) | 0.0118(4) |
| O(6) | х | 0.23315(8) | 0.23320(5) | 0.23340(8) | 0.23296(7) | 0.23307(12) | 0.23342(7) | 0.23308(7) | 0.23368(7) |
| | У | 0.5583(3) | 0.5603(2) | 0.5581(4) | 0.5585(3) | 0.5642(5) | 0.5575(3) | 0.5603(3) | 0.5556(3) |
| | Z | 0.16618(9) | 0.16554(6) | 0.16530(9) | 0.16527(7) | 0.16577(13) | 0.16511(8) | 0.16616(8) | 0.16476(9) |
| | $U_{\rm eq}$ | 0.0115(4) | 0.0120(2) | 0.0119(4) | 0.0125(3) | 0.0106(7) | 0.0130(3) | 0.0112(3) | 0.0097(4) |
| O(7) | x | 0.15428(7) | 0.15437(5) | 0.15449(8) | 0.15439(6) | 0.15426(12) | 0.15456(7) | 0.15415(7) | 0.15462(7) |
| ~ / | у | 0.9349(3) | 0.9381(2) | 0.9320(4) | 0.9376(3) | 0.9430(6) | 0.9317(3) | 0.9397(3) | 0.9287(3) |
| | Z | 0.18009(9) | 0.18009(6) | 0.18001(10) | 0.17999(7) | 0.18014(14) | 0.18005(8) | 0.18013(8) | 0.17986(9) |
| | $U_{\rm eq}$ | 0.0121(4) | 0.0126(2) | 0.0121(4) | 0.0128(3) | 0.0113(6) | 0.0133(3) | 0.0116(4) | 0.0103(4) |
| O(8) | x | 0.12108(10) | 0.12121(7) | 0.12110(11) | 0.12121(9) | 0.12103(17) | 0.12100(9) | 0.12117(9) | 0.12102(11) |
| | У | 0.4919(5) | 0.4935(3) | 0.4900(5) | 0.4917(4) | 0.4975(8) | 0.4903(4) | 0.4947(5) | 0.4879(5) |
| | Z | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| | $U_{\rm eq}$ | 0.0113(5) | 0.0110(3) | 0.0121(6) | 0.0127(4) | 0.0114(9) | 0.0127(4) | 0.0106(5) | 0.0108(5) |
| O(9) | x | 0.05802(10) | 0.05806(7) | 0.05832(11) | 0.05795(8) | 0.05789(16) | 0.05849(9) | 0.05786(9) | 0.05862(10) |
| | У | 0.9555(4) | 0.9560(3) | 0.9538(5) | 0.9553(4) | 0.9593(8) | 0.9537(4) | 0.9574(5) | 0.9523(4) |
| | Z | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| | $U_{\rm eq}$ | 0.0087(5) | 0.0093(3) | 0.0094(5) | 0.0105(4) | 0.0082(9) | 0.0106(4) | 0.0088(5) | 0.0085(5) |
| H(8) | x | 0.1627(3) | 0.1619(4) | 0.1627(3) | 0.1626(3) | 0.1606(9) | 0.1620(4) | 0.1622(4) | 0.1626(3) |
| | У | 0.459(8) | 0.441(6) | 0.4572(8) | 0.452(7) | 0.428(11) | 0.442(7) | 0.448(8) | 0.454(7) |
| | Z | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| | U _{eq} | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 |
| | | 19BAV | 21BAV | 23BAV | 25BAV | 27BAV | 28BAV | 29BAV | 31BAV |
| Ca | x | 0.08394(2) | 0.08389(2) | 0.08300(5) | 0.08388(1) | 0.08411(1) | 0.08398(2) | 0.08358(2) | 0.08362(2) |
| | У | 0.24425(7) | 0.24434(11) | 0.2506(2) | 0.24491(7) | 0.24308(6) | 0.24394(8) | 0.24703(7) | 0.24636(11) |
| | Z | 0.15255(2) | 0.15255(3) | 0.15317(5) | 0.15264(2) | 0.15241(2) | 0.15248(2) | 0.15280(2) | 0.15276(3) |
| | $U_{\rm eq}$ | 0.01119(11) | 0.01062(12) | 0.0119(3) | 0.01245(10) | 0.01111(10) | 0.011/2(11) | 0.01269(11) | 0.01103(14) |
| T(1) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | У | 0.7782(2) | 0.7782(3) | 0.7756(6) | 0.77755(18) | 0.77933(17) | 0.7785(2) | 0.77710(19) | 0.7779(3) |
| | Z | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 |
| | $U_{\rm eq}$ | 0.0077(2) | 0.0075(3) | 0.0077(6) | 0.00868(18) | 0.00781(18) | 0.0083(2) | 0.00829(19) | 0.0068(3) |
| T(2) | х | 0.12516(15) | 0.1250(2) | 0.1251(4) | 0.12506(12) | 0.12519(13) | 0.12505(16) | 0.12482(14) | 0.12497(19) |
| | У | 0.8141(7) | 0.814(1) | 0.8196(17) | 0.8139(6) | 0.8137(6) | 0.8136(7) | 0.8159(7) | 0.816(1) |
| | Z | 1/4 | $\frac{1}{4}$ | 1/4 | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | 1/4 | 1/4 |
| | $U_{\rm eq}$ | 0.0086(6) | 0.009(1) | 0.005(2) | 0.0094(5) | 0.0096(5) | 0.0098(7) | 0.0093(6) | 0.0072(9) |
| T(3) | х | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | У | 0.72302(16) | 0.7230(2) | 0.7212(6) | 0.72270(15) | 0.72297(13) | 0.72301(17) | 0.72305(17) | 0.7229(2) |
| | Z | 0.10442(4) 0.0075(2) | 0.10446(5) 0.006(3) | 0.10402(14) | 0.10440(4) | 0.10453(4) | 0.10448(4) 0.0082(2) | 0.10413(4) | 0.10423(6) |
| | Ueq | 0.0073(2) | 0.000(3) | 0.007(1) | 0.0007(2) | 0.0070(2) | 0.0003(3) | 0.0000(3) | 0.0000(4) |
| T(4) | x | 0.09529(4) | 0.09546(5) | 0.09423(10) | 0.09497(3) | 0.09553(3) | 0.09541(4) | 0.09471(3) | 0.09494(5) |
| | У | 1/2 | 1/2 | 1/2 | 1/2 | 1/2 | 1/2 | 1/2 | 1/2 |
| | Z II | 0 0 0071(2) | 0 0070(3) | 0 0067(8) | 0 0085(2) | 0 0077(2) | 0 0081(3) | 0 0075(2) | 0 0065(3) |
| | eq | 5.00/1(2) | 0.0070(3) | 0.0007(0) | 0.0000(2) | 0.00//(2) | 0.0001(0) | 0.0073(2) | 0.0005(5) |

Table 4 (contd.)

| | | 19BAV | 21BAV | 23BAV | 25BAV | 27BAV | 28BAV | 29BAV | 31BAV |
|--------------|---|--|---|---|---|--|---|--|--|
| <i>T</i> (5) | x | 0.17028(3) | 0.17025(4) | 0.17016(10) | 0.17021(3) | 0.17034(3) | 0.17026(3) | 0.17021(3) | 0.17020(4) |
| | y | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | z | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | $U_{\rm eq}$ | 0.00872(16) | 0.0085(2) | 0.0098(5) | 0.00974(14) | 0.00878(14) | 0.00938(17) | 0.00968(15) | 0.0080(2) |
| <i>T</i> (6) | x | 0.21415(2) | 0.21412(3) | 0.21386(7) | 0.21413(2) | 0.21415(2) | 0.21413(2) | 0.21409(2) | 0.21410(3) |
| | y | 0.85518(10) | 0.85569(14) | 0.8603(3) | 0.85570(9) | 0.85448(9) | 0.85503(11) | 0.85745(10) | 0.85725(14) |
| | z | 0.14322(3) | 0.14323(3) | 0.14393(7) | 0.14332(2) | 0.14301(2) | 0.14315(3) | 0.14361(2) | 0.14345(3) |
| | U _{eq} | 0.00814(13) | 0.00785(15) | 0.0083(3) | 0.00903(11) | 0.00838(11) | 0.00878(13) | 0.00865(12) | 0.00717(16) |
| O(1) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.5750(4) | 0.5758(5) | 0.5755(9) | 0.5751(3) | 0.5751(3) | 0.5755(4) | 0.5750(4) | 0.5754(5) |
| | z | 0.18271(9) | 0.18297(11) | 0.1831(3) | 0.18258(9) | 0.18274(8) | 0.18293(10) | 0.18243(9) | 0.18264(12) |
| | U _{eq} | 0.0099(4) | 0.0089(5) | 0.0092(12) | 0.0106(3) | 0.0099(3) | 0.0100(4) | 0.0103(4) | 0.0085(5) |
| O(2) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.0350(4) | 0.0363(5) | 0.0382(9) | 0.0346(4) | 0.0354(3) | 0.0354(4) | 0.0355(4) | 0.0359(5) |
| | z | 0.11309(10) | 0.11309(12) | 0.1108(3) | 0.11255(9) | 0.11354(9) | 0.11329(11) | 0.11164(10) | 0.11197(13) |
| | U _{eq} | 0.0118(4) | 0.0111(5) | 0.0129(13) | 0.0136(3) | 0.0119(3) | 0.0127(4) | 0.0126(4) | 0.0108(5) |
| O(3) | x | 0.05752(6) | 0.05764(8) | 0.05737(16) | 0.05739(5) | 0.05761(5) | 0.05763(6) | 0.05747(5) | 0.05752(8) |
| | y | 0.5995(3) | 0.5991(3) | 0.5942(7) | 0.5988(2) | 0.5998(2) | 0.5998(3) | 0.5982(3) | 0.5988(4) |
| | z | 0.07113(7) | 0.07132(8) | 0.06987(18) | 0.07101(7) | 0.07149(7) | 0.07138(8) | 0.07027(7) | 0.07061(9) |
| | U _{eq} | 0.0136(3) | 0.0123(4) | 0.0112(9) | 0.0152(3) | 0.0137(3) | 0.0140(3) | 0.0148(3) | 0.0126(4) |
| O(4) | x | 0.13125(6) | 0.13157(7) | 0.13128(15) | 0.13109(6) | 0.13148(5) | 0.13145(6) | 0.13104(6) | 0.13131(8) |
| | y | 0.2317(3) | 0.2307(4) | 0.2360(7) | 0.2325(2) | 0.2302(2) | 0.2311(3) | 0.2348(3) | 0.2333(4) |
| | z | 0.03601(7) | 0.03596(9) | 0.03429(17) | 0.03575(7) | 0.03639(6) | 0.03606(8) | 0.03515(7) | 0.03538(10) |
| | U _{eq} | 0.0131(3) | 0.0118(4) | 0.0128(8) | 0.0141(3) | 0.0123(3) | 0.0131(3) | 0.0140(3) | 0.0126(4) |
| O(5) | x | 0.20830(6) | 0.20836(8) | 0.20816(16) | 0.20829(5) | 0.20829(5) | 0.20825(6) | 0.20829(5) | 0.20825(7) |
| | y | 0.8648(3) | 0.8644(4) | 0.8698(7) | 0.8655(2) | 0.8640(2) | 0.8642(3) | 0.8673(3) | 0.8663(4) |
| | z | 0.06005(7) | 0.06003(8) | 0.06059(17) | 0.06025(6) | 0.05992(6) | 0.05994(7) | 0.06048(6) | 0.06026(9) |
| | U _{eq} | 0.0125(3) | 0.0124(4) | 0.0126(8) | 0.0138(3) | 0.0127(2) | 0.0132(3) | 0.0138(3) | 0.0122(4) |
| O(6) | x | 0.23353(6) | 0.23378(8) | 0.23354(15) | 0.23343(5) | 0.23361(5) | 0.23358(6) | 0.23337(5) | 0.23336(8) |
| | y | 0.5551(3) | 0.5563(3) | 0.5601(6) | 0.5556(2) | 0.5549(2) | 0.5556(3) | 0.5573(3) | 0.5572(4) |
| | z | 0.16495(7) | 0.16470(8) | 0.16556(18) | 0.16518(6) | 0.16479(6) | 0.16475(7) | 0.16539(6) | 0.16516(9) |
| | U _{eq} | 0.0111(3) | 0.0102(4) | 0.0109(9) | 0.0125(3) | 0.0116(2) | 0.0115(3) | 0.0119(3) | 0.0104(4) |
| O(7) | x | 0.15456(6) | 0.15469(7) | 0.15479(15) | 0.15456(5) | 0.15464(5) | 0.15463(6) | 0.15439(5) | 0.15452(8) |
| | y | 0.9298(3) | 0.9292(4) | 0.9346(7) | 0.9307(2) | 0.9288(2) | 0.9291(3) | 0.9324(3) | 0.9314(4) |
| | z | 0.17998(7) | 0.17972(8) | 0.17973(18) | 0.18002(6) | 0.18000(6) | 0.17986(7) | 0.18002(7) | 0.17988(9) |
| | U _{eq} | 0.0112(3) | 0.0111(4) | 0.0107(8) | 0.0127(3) | 0.0119(3) | 0.0120(3) | 0.0123(3) | 0.0103(4) |
| O(8) | x y z | 0.12113(8) 0.4883(4) ¹ / ₄ | 0.12100(11) 0.4885(5) ¹ / ₄ | $\begin{array}{c} 0.1205(2) \\ 0.492(1) \\ \frac{1}{4} \\ 0.0024(44) \end{array}$ | 0.12116(7) 0.4884(3) ¹ / ₄ | $\begin{array}{c} 0.12104(7) \\ 0.4877(3) \\ \frac{1}{4} \\ 0.0110(2) \end{array}$ | 0.12109(8) 0.4879(4) ¹ / ₄ | $\begin{array}{c} 0.12114(7) \\ 0.4897(4) \\ \frac{1}{4} \\ 0.0110(4) \end{array}$ | 0.12093(11) 0.4900(5) ¹ / ₄ |
| - | $U_{\rm eq}$ | 0.0112(4) | 0.0115(5) | 0.0094(11) | 0.0122(3) | 0.0118(3) | 0.0123(4) | 0.0119(4) | 0.0102(5) |
| O(9) | x y z | $0.05864(8) \\ 0.9528(4) \\ \frac{1}{4} \\ 0.0005(4)$ | 0.05853(11) 0.9526(5) $\frac{1}{4}$ | $\begin{array}{c} 0.0585(2) \\ 0.955(1) \\ {}^{1}\!\!\!/_{4} \\ 0.0102(12) \end{array}$ | $\begin{array}{c} 0.05854(7) \\ 0.9529(3) \\ \frac{1}{4} \\ 0.0102(2) \end{array}$ | $\begin{array}{c} 0.05876(7) \\ 0.9523(3) \\ \frac{1}{4} \\ 0.0005(2) \end{array}$ | $\begin{array}{c} 0.05870(8) \\ 0.9523(4) \\ \frac{1}{4} \\ 0.0101(1) \end{array}$ | 0.05842(7) 0.9540(4) $\frac{1}{4}$ | 0.05851(10) 0.9533(5) $\frac{1}{4}$ |
| H(8) | U _{eq} x y z U _{eq} | $\begin{array}{c} 0.0095(4)\\ 0.1629(2)\\ 0.461(6)\\ {}^{1}\!$ | 0.1091(5) 0.1625(3) 0.453(8) ¹ / ₄ 0.015* | 0.1601(11) 0.424(13) ¹ / ₄ 0.015* | $\begin{array}{c} 0.0102(3) \\ 0.1624(3) \\ 0.4458(9) \\ \frac{1}{4} \\ 0.015* \end{array}$ | 0.1095(3) 0.1626(2) 0.453(6) ¹ / ₄ 0.015* | $\begin{array}{c} 0.0101(4) \\ 0.1624(3) \\ 0.448(7) \\ \frac{1}{4} \\ 0.015^{*} \end{array}$ | 0.0097(3) 0.1625(3) 0.44942(11) $\frac{1}{4}$ 0.015* | 0.1627(3) 0.463(9) ¹ / ₄ 0.015* |

Table 4 (contd.)

| | | 32BAV | 33BAV | 35BAV | 36ABAV | 37BAV | 39BAV | 40BAV | 41BAV |
|--------------|--------------------------------|--|--|---|---|--|--|--|---|
| Ca | x | 0.08269(2) | 0.08406(2) | 0.08173(5) | 0.08377(3) | 0.08346(2) | 0.08366(2) | 0.08215(2) | 0.08367(4) |
| | y | 0.25323(11) | 0.24351(9) | 0.2584(3) | 0.24583(14) | 0.24646(10) | 0.2466(10) | 0.25394(11) | 0.2462(2) |
| | z | 0.15349(3) | 0.15246(2) | 0.15440(6) | 0.15279(3) | 0.15288(2) | 0.15275(3) | 0.15377(3) | 0.15286(5) |
| | U _{eq} | 0.01248(13) | 0.01240(13) | 0.0127(3) | 0.01111(16) | 0.01205(12) | 0.01178(13) | 0.01369(13) | 0.0108(2) |
| <i>T</i> (1) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.7748(3) | 0.7790(2) | 0.7744(7) | 0.7784(4) | 0.7775(3) | 0.7779(3) | 0.7721(3) | 0.7773(6) |
| | z | $\frac{1}{4}$ | $\frac{1}{4}$ | ¹ / ₄ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | ¹ / ₄ | ¹ / ₄ |
| | Uco | 0.0074(3) | 0.0091(2) | 0.0065(6) | 0.0069(3) | 0.0077(2) | 0.0079(3) | 0.0090(3) | 0.0071(5) |
| <i>T</i> (2) | x y z | $0.12453(19) \\ 0.8206(9) \\ \frac{1}{4} \\ 0.0090(8)$ | 0.12507(17) 0.8133(8) ¹ / ₄ 0.0096(7) | $\begin{array}{c} 0.1242(5) \\ 0.828(2) \\ \frac{1}{4} \\ 0.010(2) \end{array}$ | $\begin{array}{c} 0.1248(2) \\ 0.8151(12) \\ \frac{1}{4} \\ 0.007(1) \end{array}$ | 0.12486(17) 0.8144(8) ¹ / ₄ 0.0087(8) | 0.12468(18) 0.8160(9) ¹ / ₄ 0.0079(8) | 0.12437(17) 0.8208(9) $\frac{1}{4}$ 0.0063(7) | $0.1250(4) \\ 0.8151(17) \\ \frac{1}{4} \\ 0.0061(15)$ |
| <i>T</i> (3) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.7218(3) | 0.72308(19) | 0.7204(9) | 0.7223(3) | 0.7229(2) | 0.7231(2) | 0.7201(2) | 0.7211(5) |
| | z | 0.10384(7) | 0.10456(5) | 0.1030(2) | 0.10425(7) | 0.10424(5) | 0.10413(6) | 0.10421(8) | 0.10440(12) |
| | U _{eq} | 0.0076(5) | 0.0090(3) | 0.0105(13) | 0.0065(4) | 0.0078(3) | 0.0075(3) | 0.0095(5) | 0.0066(7) |
| <i>T</i> (4) | x y z U _{eq} | $0.09378(4) \\ \frac{1/2}{0} \\ 0.0065(3)$ | $\begin{array}{c} 0.09524(4) \\ \frac{1}{2} \\ 0 \\ 0.0090(3) \end{array}$ | $\begin{array}{c} 0.09319(10) \\ \frac{1}{2} \\ 0 \\ 0.0070(7) \end{array}$ | $0.09506(6) \\ \frac{1}{2} \\ 0 \\ 0.0068(4)$ | $\begin{array}{c} 0.09493(4) \\ \frac{1}{2} \\ 0 \\ 0.0066(3) \end{array}$ | $\begin{array}{c} 0.09497(4) \\ \frac{1}{2} \\ 0 \\ 0.0063(3) \end{array}$ | $\begin{array}{c} 0.09375(4) \\ \frac{1}{2} \\ 0 \\ 0.0070(3) \end{array}$ | 0.09468(9) ¹ / ₂ 0 0.0066(6) |
| <i>T</i> (5) | x | 0.17030(4) | 0.17018(4) | 0.16995(10) | 0.17040(5) | 0.17018(4) | 0.17032(4) | 0.17016(4) | 0.17044(8) |
| | y | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | z | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | U _{eq} | 0.0090(2) | 0.00998(19) | 0.0081(5) | 0.0079(2) | 0.00810(18) | 0.0090(2) | 0.00972(19) | 0.0079(4) |
| <i>T</i> (6) | x | 0.21400(3) | 0.21414(3) | 0.21375(7) | 0.21418(4) | 0.21410(3) | 0.21415(3) | 0.21392(3) | 0.21420(6) |
| | y | 0.86186(14) | 0.85474(12) | 0.8671(3) | 0.85648(18) | 0.85831(12) | 0.85694(13) | 0.86269(13) | 0.8562(3) |
| | z | 0.14435(3) | 0.14310(3) | 0.14453(7) | 0.14350(4) | 0.14347(3) | 0.14362(3) | 0.14405(3) | 0.14357(7) |
| | U _{eq} | 0.00779(15) | 0.00942(14) | 0.0067(3) | 0.00737(18) | 0.00775(14) | 0.00777(15) | 0.00865(15) | 0.0069(3) |
| O(1) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.5748(5) | 0.5751(4) | 0.5745(12) | 0.5757(7) | 0.5755(5) | 0.5755(5) | 0.5729(5) | 0.5750(10) |
| | z | 0.18221(12) | 0.18272(11) | 0.1818(3) | 0.18264(17) | 0.18268(12) | 0.18262(12) | 0.18240(13) | 0.1824(3) |
| | U _{eq} | 0.0094(5) | 0.0114(4) | 0.0101(12) | 0.0097(6) | 0.0097(4) | 0.0100(5) | 0.0113(5) | 0.010(1) |
| O(2) | x | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | y | 0.0365(5) | 0.0347(5) | 0.0359(12) | 0.0367(7) | 0.0368(5) | 0.0371(5) | 0.0354(5) | 0.0356(10) |
| | z | 0.10951(13) | 0.11328(12) | 0.1083(3) | 0.11201(18) | 0.11203(13) | 0.11200(13) | 0.10949(15) | 0.1120(3) |
| | U _{eq} | 0.0119(5) | 0.0136(5) | 0.0121(13) | 0.0115(7) | 0.0128(5) | 0.0123(5) | 0.0145(5) | 0.0117(10) |
| O(3) | x | 0.05758(7) | 0.05741(7) | 0.05761(17) | 0.05756(11) | 0.05757(7) | 0.05757(7) | 0.05753(8) | 0.05735(16) |
| | y | 0.5959(4) | 0.5993(3) | 0.5933(9) | 0.5985(5) | 0.5985(3) | 0.5991(3) | 0.5955(4) | 0.5982(8) |
| | z | 0.06888(9) | 0.07145(8) | 0.06826(19) | 0.07053(13) | 0.07051(9) | 0.07021(9) | 0.06913(10) | 0.07057(19) |
| | U _{eq} | 0.0134(4) | 0.0149(3) | 0.0127(9) | 0.0133(5) | 0.0135(4) | 0.0135(4) | 0.0151(4) | 0.0136(7) |
| O(4) | x | 0.13074(7) | 0.13141(7) | 0.13070(17) | 0.13117(11) | 0.13129(7) | 0.13122(7) | 0.13086(8) | 0.13109(16) |
| | y | 0.2393(4) | 0.2309(3) | 0.2415(9) | 0.2334(5) | 0.2331(3) | 0.2343(3) | 0.2387(4) | 0.2339(8) |
| | z | 0.03352(9) | 0.03626(8) | 0.0323(2) | 0.03555(12) | 0.03518(9) | 0.03513(9) | 0.03381(10) | 0.03546(18) |
| | U _{eq} | 0.0141(4) | 0.0138(3) | 0.0131(9) | 0.0127(5) | 0.0127(3) | 0.0130(4) | 0.0147(4) | 0.0124(7) |
| O(5) | x | 0.20825(7) | 0.20825(6) | 0.20778(18) | 0.20826(10) | 0.20816(7) | 0.20827(7) | 0.20814(8) | 0.20812(15) |
| | y | 0.8724(4) | 0.8637(3) | 0.8789(9) | 0.8659(5) | 0.8673(3) | 0.8660(3) | 0.8735(4) | 0.8654(8) |
| | z | 0.06123(9) | 0.05998(8) | 0.06122(18) | 0.06041(12) | 0.06037(8) | 0.06043(9) | 0.06087(9) | 0.06044(17) |
| | U _{eq} | 0.0137(4) | 0.0140(3) | 0.0121(9) | 0.0123(5) | 0.0121(3) | 0.0128(4) | 0.0139(4) | 0.0114(7) |

Table 4 (contd.)

| | | 32BAV | 33BAV | 35BAV | 36ABAV | 37BAV | 39BAV | 40BAV | 41BAV |
|------|--------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| O(6) | x | 0.23303(8) | 0.23346(7) | 0.23297(17) | 0.23347(10) | 0.23366(7) | 0.23345(7) | 0.23313(8) | 0.23336(15) |
| | у | 0.5597(4) | 0.5552(3) | 0.5654(8) | 0.5563(5) | 0.5584(3) | 0.5568(3) | 0.5602(4) | 0.5558(7) |
| | Ζ | 0.16607(9) | 0.16476(8) | 0.16575(19) | 0.16528(12) | 0.16507(9) | 0.16530(9) | 0.16560(9) | 0.16547(18) |
| | $U_{\rm eq}$ | 0.0110(4) | 0.0124(3) | 0.0092(9) | 0.0109(5) | 0.0110(3) | 0.0111(4) | 0.0123(4) | 0.0099(7) |
| O(7) | x | 0.15429(7) | 0.15457(7) | 0.15418(17) | 0.15458(10) | 0.15459(7) | 0.15446(7) | 0.15435(7) | 0.15447(15) |
| | y | 0.9380(4) | 0.9287(3) | 0.9434(8) | 0.9314(5) | 0.9319(3) | 0.93122(3) | 0.9394(4) | 0.9310(7) |
| | Z | 0.18013(9) | 0.18000(8) | 0.1802(2) | 0.18011(12) | 0.17991(9) | 0.17990(9) | 0.18036(9) | 0.18009(18) |
| | $U_{\rm eq}$ | 0.0110(4) | 0.0127(3) | 0.0101(9) | 0.0108(5) | 0.0113(3) | 0.0112(4) | 0.0125(4) | 0.0100(7) |
| O(8) | x | 0.12109(10) | 0.12101(10) | 0.1211(2) | 0.12101(14) | 0.12103(10) | 0.12107(10) | 0.12132(11) | 0.1209(2) |
| | v | 0.4938(5) | 0.4881(4) | 0.4980(12) | 0.4902(7) | 0.4898(5) | 0.4888(5) | 0.4939(5) | 0.4898(11) |
| | Z | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 |
| | $U_{\rm eq}$ | 0.0109(5) | 0.0128(4) | 0.0096(11) | 0.0107(6) | 0.0116(5) | 0.0113(5) | 0.0121(5) | 0.0101(9) |
| O(9) | x | 0.05811(10) | 0.05877(9) | 0.0578(2) | 0.05859(13) | 0.05841(9) | 0.05830(10) | 0.05801(10) | 0.0587(2) |
| | y | 0.9564(5) | 0.9524(4) | 0.9574(12) | 0.9530(7) | 0.9532(5) | 0.9538(5) | 0.9554(5) | 0.9525(10) |
| | Z | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 |
| | $U_{\rm eq}$ | 0.0083(5) | 0.0099(4) | 0.0079(12) | 0.0078(6) | 0.0092(4) | 0.0087(5) | 0.0093(5) | 0.0072(9) |
| H(8) | x | 0.1625(4) | 0.1628(3) | 0.1602(15) | 0.1601(12) | 0.1615(5) | 0.1630(2) | 0.1617(6) | 0.1603(15) |
| . / | v | 0.4554(7) | 0.460(7) | 0.425(17) | 0.427(12) | 0.435(8) | 0.466(8) | 0.43(1) | 0.420(18) |
| | Z | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 | 1/4 |
| | $U_{\rm eq}$ | 0.015* | 0.015* | 0.015* | 0.015* | 0.015* | 0.015* | 0.015* | 0.015* |

2002): 1.55 and 1.82 v.u. for O(2) and 1.14 and 1.08 v.u. for O(8). These values indicate that the O(8) site is occupied completely by (OH) and the O(2) site is occupied by both (OH) and O^{2-} . The position of the H atom associated with the O atom at the O(8) site is shown in detail in Fig. 6. The O–H bond projects out into the cavity between the chains of *T*(6) tetrahedra which extend in the **b** direction (Fig. 6) and there is a hydrogen bond to the O(6) anion that links adjacent *T*(6) tetrahedra.

We were not able to locate the partly occupied H site adjacent to the O(2) anion in difference-Fourier maps in the final stages of refinement. However, space requirements constrain the H atom to lie as indicated in Fig. 7. There are three anions which could possibly act as acceptor anions for a hydrogen bond: O(1), O(3) and O(4). The corresponding anion-anion separations are as follows: $O(2)-O(1) \approx 3.05$, $O(2)-O(3) \approx$ 3.24, O(2)–O(4) \approx 3.54 Å. All these distances are edges of the Ca polyhedron, and hydrogen bonds along the edge of a coordination polyhedron are extremely unusual; however, these are the only possibilities. All distances are reasonable Odonor-Oacceptor distances for a hydrogen bond, but O(3) as a hydrogen-bond acceptor is more in accord with local bond-valence requirements (see later discussion). Ideally, the H atom will occur on a mirror plane and will form a bifurcated bond to two symmetry-related O(3) anions. However, the occupancies of the associated symmetryrelated pairs of T(3) sites and T(4) sites do not necessarily obey the long-range symmetry of the structure, and the H(2) atom may be disordered off its special position to form a single hydrogen bond to one of the locally associated O(3) anions.

Chemical composition

As is apparent from Fig. 5, there is extensive solid-solution described by the following exchange: $^{T(4)}Si + ^{T(3)}Be + ^{O(2)}OH^- \rightleftharpoons ^{T(4)}Al + ^{T(3)}Si + ^{O(2)}O^{2-}$. It is also apparent from this expression that chemical variation in bavenite involves the T(3), T(4) and O(2) sites, and the remaining sites in the structure have fixed composition (except for minor substitution of Na for Ca at the *Ca* site). Thus we may write the chemical formula of the fixed part of the structure as Ca₄Be₂Si₇O₂₄(OH)₂ and the chemical formula of the variable part of the structure as [(Be,Si)₂(Si,Al)₂(OH,O)₂]. The latter part of the complete formula emphasizes that there are two end-members involved in the bavenite solid-



FIG. 1. The crystal structure of bavenite projected down b; (a) four-membered rings of (Si,Be)O₄ [T(3), pink] and (Si,Al)O₄ [T(4), green] tetrahedra alternating with six-membered rings of SiO₄ tetrahedra [T(5), T(6), mauve] forming a chain that extends in the **a** direction; (b) chain of Fig. 1a linked in the **c** direction by linear BeO₄-SiO₄-BeO₄ [T(2) yellow-T(1) mauve-T(2)] trimers.

solution series: $Ca_4Be_2Si_7O_{24}(OH)_2$ [$Be_2Si_2(OH)_2$] and $Ca_4Be_2Si_7O_{24}(OH)_2$ [$Si_2Al_2O_2$]; this issue is dealt with below. We may also write the general formula of the bavenite solid-solution series as $Ca_4Be_2Si_7O_{24}(OH)_2$ [($Be_3Si_2(Si_3Al)_2(OH,O)_2$] where the variable part of the formula is written in square brackets.

Beus (1966) wrote the bavenite series as between the compositions $Ca_4Be_2Si_7O_{24}(OH)_2$ [BeA1Si₂(OH)O] and $Ca_4Be_2Si_7O_{24}(OH)_2$ [Si₂Al₂O₂]. As is apparent from Fig. 8, the compositions of the current work span this range, but they extend slightly beyond the value of Be = 3 a.p.f.u. to 3.13 a.p.f.u. (from Baveno, Italy) and 3.12 a.p.f.u. (from Mont Saint-Hilaire, Canada); moreover, the former value is supported by the smallest *b* dimension of those recorded here (Fig. 8). However, these two samples are also characterized by another compositional feature: as shown in Fig. 9, they also have small but significant amounts of Na replacing Ca at the *Ca* site. This suggests that Be may increase past the value of 3 a.p.f.u., but only involving substitution of Na for Ca. It seems that the limit to solidsolution suggested by Beus (1966) is quite strict, and that greater contents of Be can occur only through a different substitution mechanism.

Short-range order in bavenite

The results of crystal-structure refinement give us an average picture of the atomic arrangement in a crystal, and bond-valence arguments generally apply to this average arrangement. However, bond-valence theory also applies to the local structure in a crystal (Hawthorne, 1997) and can

| 25BAV | $\begin{array}{c} 2.619(1) \\ 2.347(1) \\ 2.456(1) \\ 2.524(1) \end{array}$ | $\begin{array}{c} 2.334(1) \\ 2.412(1) \\ 2.463(1) \\ 2.451 \end{array}$ | $\begin{array}{c} 1.657(2) \\ 1.618(2) \\ 1.638 \end{array}$ | $\begin{array}{c} 1.632(2) \\ 1.632(3) \\ 1.693(3) \\ 1.647 \end{array}$ | 1.690(2) 1.569(2) 1.607(1) 1.618 | $\begin{array}{c} 1.706(1) \\ 1.726(1) \\ 1.716 \end{array}$ | $\begin{array}{c} 1.631(1) \\ 1.615(1) \\ 1.623 \end{array}$ | $\begin{array}{c} 1.622(1)\\ 1.624(1)\\ 1.632(1)\\ 1.601(1)\\ 1.620\end{array}$ |
|-------------|---|--|--|--|--|--|--|--|
| 23BAV | 2.582(3) 2.346(3) 2.429(4) 2.567(4) | 2.350(4) 2.395(3) 2.455(3) 2.446 | $\begin{array}{c} 1.637(5) \\ 1.625(5) \\ 1.631 \end{array}$ | $\begin{array}{c} 1.632(6)\\ 1.64(1)\\ 1.69(1)\\ 1.648\end{array}$ | 1.699(6) 1.586(6) 1.616(4) 1.629 | $1.671(4) \\ 1.707(4) \\ 1.689$ | 1.625(4) 1.607(4) 1.616 | $\begin{array}{c} 1.624(4)\\ 1.620(3)\\ 1.620(4)\\ 1.630(4)\\ 1.581(4)\\ 1.614\end{array}$ |
| 21BAV | 2.626(2) 2.338(2) 2.454(2) 2.523(2) | 2.339(2) 2.414(2) 2.464(2) 2.451 | $\begin{array}{c} 1.651(2) \\ 1.615(3) \\ 1.633 \end{array}$ | $\begin{array}{c} 1.636(3) \\ 1.632(5) \\ 1.692(5) \\ 1.649 \end{array}$ | $\begin{array}{c} 1.695(3)\\ 1.578(3)\\ 1.609(2)\\ 1.623\end{array}$ | 1.715(2) 1.735(2) 1.725 | 1.622(2) 1.614(2) 1.618 | $\begin{array}{c} 1.624(2)\\ 1.622(2)\\ 1.622(2)\\ 1.627(2)\\ 1.594(2)\\ 1.617\end{array}$ |
| 19BAV | $\begin{array}{c} 2.623(1) \\ 2.341(1) \\ 2.459(1) \\ 2.519(1) \end{array}$ | 2.334(1) 2.414(1) 2.463(1) 2.450 | 1.657(2) 1.617(2) 1.637 | $\begin{array}{c} 1.629(2) \\ 1.634(4) \\ 1.693(4) \\ 1.646 \end{array}$ | $\begin{array}{c} 1.693(2) \\ 1.571(2) \\ 1.607(1) \\ 1.620 \end{array}$ | $\begin{array}{c} 1.712(1) \\ 1.730(1) \\ 1.721 \end{array}$ | $\begin{array}{c} 1.630(1) \\ 1.612(1) \\ 1.621 \end{array}$ | $\begin{array}{c} 1.624(1)\\ 1.624(1)\\ 1.624(2)\\ 1.629(2)\\ 1.601(1)\\ 1.620\end{array}$ |
| 15BAV | 2.632(2) 2.337(2) 2.459(2) 2.515(2) | 2.334(2) 2.415(2) 2.465(2) 2.451 | $\begin{array}{c} 1.657(2) \\ 1.612(2) \\ 1.635 \end{array}$ | $\begin{array}{c} 1.633(3)\\ 1.636(5)\\ 1.686(5)\\ 1.647\end{array}$ | $\begin{array}{c} 1.695(3) \\ 1.578(2) \\ 1.607(2) \\ 1.622 \end{array}$ | $\begin{array}{c} 1.720(2) \\ 1.738(2) \\ 1.729 \end{array}$ | 1.623(2) 1.612(2) 1.618 | $\begin{array}{c} 1.625(2)\\ 1.623(2)\\ 1.629(2)\\ 1.599(2)\\ 1.619\end{array}$ |
| 14BAV | 2.549(2) 2.363(2) 2.432(2) 2.585(2) | 2.342(2) 2.396(2) 2.453(2) 2.446 | $\begin{array}{c} 1.652(2) \\ 1.622(2) \\ 1.637 \end{array}$ | $\begin{array}{c} 1.630(3) \\ 1.629(5) \\ 1.684(5) \\ 1.643 \end{array}$ | $\begin{array}{c} 1.688(3) \\ 1.565(3) \\ 1.624(2) \\ 1.625 \end{array}$ | $1.639(2) \\ 1.678(2) \\ 1.659$ | $\begin{array}{c} 1.641(2) \\ 1.608(2) \\ 1.625 \end{array}$ | $\begin{array}{c} 1.623(2)\\ 1.623(2)\\ 1.629(2)\\ 1.598(2)\\ 1.618\end{array}$ |
| 13BAV | $\begin{array}{c} 2.610(1) \\ 2.344(1) \\ 2.451(2) \\ 2.538(2) \end{array}$ | 2.340(2) 2.413(1) 2.461(1) 2.451 | $\begin{array}{c} 1.655(2) \\ 1.619(2) \\ 1.637 \end{array}$ | $\begin{array}{c} 1.632(2) \\ 1.633(4) \\ 1.686(4) \\ 1.646 \end{array}$ | 1.692(2) 1.575(2) 1.616(2) 1.625 | $\begin{array}{c} 1.696(2) \\ 1.724(2) \\ 1.710 \end{array}$ | $\begin{array}{c} 1.628(2) \\ 1.611(2) \\ 1.620 \end{array}$ | $\begin{array}{c} 1.623(2)\\ 1.623(2)\\ 1.623(2)\\ 1.632(2)\\ 1.598(2)\\ 1.619\end{array}$ |
| 12BAV | $\begin{array}{c} 2.525(3) \\ 2.365(3) \\ 2.423(3) \\ 2.631(3) \end{array}$ | 2.350(3) 2.390(3) 2.442(3) 2.447 | $\begin{array}{c} 1.641(4) \\ 1.632(4) \\ 1.637 \end{array}$ | 1.638(5) 1.620(9) 1.677(8) 1.643 | 1.693(5) 1.568(5) 1.626(3) 1.628 | $1.632(3) \\ 1.674(3) \\ 1.653$ | $\begin{array}{c} 1.629(3) \\ 1.596(3) \\ 1.613 \end{array}$ | $\begin{array}{c} 1.625(3)\\ 1.622(3)\\ 1.622(3)\\ 1.628(3)\\ 1.589(3)\\ 1.616\end{array}$ |
| 11BAV | 2.552(2) 2.350(1) 2.426(2) 2.576(2) | 2.344(2) 2.401(1) 2.455(1) 2.443 | $1.651(2) \\ 1.624(2) \\ 1.637$ | $\begin{array}{c} 1.635(3) \\ 1.639(5) \\ 1.677(4) \\ 1.647 \end{array}$ | $\begin{array}{c} 1.679(2) \\ 1.563(2) \\ 1.625(2) \\ 1.623 \end{array}$ | $\begin{array}{c} 1.661(2) \\ 1.705(2) \\ 1.683 \end{array}$ | $\begin{array}{c} 1.625(2) \\ 1.603(2) \\ 1.614 \end{array}$ | $\begin{array}{c} 1.624(2)\\ 1.623(2)\\ 1.630(2)\\ 1.594(2)\\ 1.618\end{array}$ |
| 10BAV | 2.600(2) 2.348(2) 2.449(2) 2.548(2) | 2.342(2) 2.406(2) 2.461(2) 2.451 | $\begin{array}{c} 1.655(3) \\ 1.615(3) \\ 1.635 \end{array}$ | $\begin{array}{c} 1.629(3) \\ 1.637(5) \\ 1.686(5) \\ 1.645 \end{array}$ | $\begin{array}{c} 1.688(3)\\ 1.571(3)\\ 1.618(2)\\ 1.624\end{array}$ | $\begin{array}{c} 1.684(2) \\ 1.713(2) \\ 1.699 \end{array}$ | $\begin{array}{c} 1.628(2) \\ 1.611(2) \\ 1.620 \end{array}$ | $\begin{array}{c} 1.622(2)\\ 1.621(2)\\ 1.631(2)\\ 1.631(2)\\ 1.595(2)\\ 1.617\end{array}$ |
| 7BAV | 2.563(1) 2.356(1) 2.431(1) 2.576(1) | 2.343(1) 2.402(1) 2.455(1) 2.447 | $1.650(2) \\ 1.622(2) \\ 1.636$ | $\begin{array}{c} 1.634(2) \\ 1.634(3) \\ 1.678(3) \\ 1.645 \end{array}$ | $\begin{array}{c} 1.681(2) \\ 1.574(2) \\ 1.624(1) \\ 1.626 \end{array}$ | $\begin{array}{c} 1.663(1) \\ 1.701(1) \\ 1.682 \end{array}$ | $\begin{array}{c} 1.631(1) \\ 1.606(1) \\ 1.618 \end{array}$ | $\begin{array}{c} 1.624(1)\\ 1.622(1)\\ 1.630(1)\\ 1.596(1)\\ 1.618\end{array}$ |
| 2ABAV | 2.581(2) 2.359(2) 2.451(2) 2.565(2) | 2.340(2) 2.399(2) 2.459(2) 2.451 | $\begin{array}{c} 1.655(2) \\ 1.616(2) \\ 1.636 \end{array}$ | $\begin{array}{c} 1.629(3) \\ 1.631(5) \\ 1.688(5) \\ 1.644 \end{array}$ | $\begin{array}{c} 1.690(3)\\ 1.571(3)\\ 1.618(2)\\ 1.624\end{array}$ | 1.661(2) 1.683(2) 1.672 | 1.645(2) 1.615(2) 1.630 | $\begin{array}{c} 1.622(2)\\ 1.621(2)\\ 1.631(2)\\ 1.598(2)\\ 1.619\end{array}$ |
| | | | $\stackrel{\times}{}_{22}$ | × 2 | × 2 | $\stackrel{\times}{}_{2}$ | $\stackrel{\times}{}_{2}$ | |
| | Ca - 0(1) Ca - 0(2) Ca - 0(3) Ca - 0(4) | Ca = 0(7) Ca = 0(8) Ca = 0(9) < Ca = 0> | T(1)-O(1) T(1)-O(9) < T(1)-O> | T(2) - O(7) T(2) - O(8) T(2) - O(9) < T(2) - O> | T(3)-O(1) T(3)-O(2) T(3)-O(3) < T(3)-O> | T(4)-O(3) T(4)-O(4) < T(4)-O> | T(5)-O(4) T(5)-O(5) < T(5)-O> | $\begin{array}{c} T(6)-O(5)\\ T(6)-O(6)\\ T(6)-O(6)\\ T(6)-O(6)\\ T(6)-O(7)\\ \end{array}$ |

 T_{ABLE} 5. Selected interatomic distances (\mathring{A}) in bavenite.

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| 41BAV | 2.606(4) 2.346(3) 2.453(3) 2.533(4) 2.533(4) 2.336(4) 2.406(4) 2.449 | $\begin{array}{c} 1.657(5) \\ 1.618(5) \\ 1.638 \end{array}$ | $\begin{array}{c} 1.627(6) \\ 1.627(10) \\ 1.683(10) \\ 1.641 \end{array}$ | 1.681(6) 1.578(6) 1.606(4) 1.618 | 1.694(4) 1.719(4) 1.707 | $\begin{array}{c} 1.634(4) \\ 1.611(4) \\ 1.623 \end{array}$ | 1.622(4) 1.622(4) 1.629(4) 1.601(4) 1.619 |
|--------|--|--|---|--|--|--|--|
| 40BAV | 2.54(2) 2.356(2) 2.433(2) 2.593(2) 2.593(2) 2.349(2) 2.348(2) 2.446 | $\begin{array}{c} 1.646(3) \\ 1.625(3) \\ 1.636 \end{array}$ | $\begin{array}{c} 1.633(3) \\ 1.627(5) \\ 1.678(5) \\ 1.643 \end{array}$ | $\begin{array}{c} 1.688(3) \\ 1.572(3) \\ 1.621(2) \\ 1.626 \end{array}$ | $\begin{array}{c} 1.655(2) \\ 1.692(2) \\ 1.674 \end{array}$ | $1.635(2) \\ 1.604(2) \\ 1.620$ | $\begin{array}{c} 1.624(2)\\ 1.624(2)\\ 1.627(2)\\ 1.598(2)\\ 1.618\end{array}$ |
| 39BAV | 2.610(2) 2.344(2) 2.459(2) 2.539(2) 2.337(2) 2.462(2) 2.462(2) 2.451 | $\begin{array}{c} 1.655(2) \\ 1.614(2) \\ 1.635 \end{array}$ | $\begin{array}{c} 1.633(3) \\ 1.638(5) \\ 1.687(5) \\ 1.648 \end{array}$ | $\begin{array}{c} 1.695(3) \\ 1.577(3) \\ 1.614(2) \\ 1.625 \end{array}$ | $\begin{array}{c} 1.691(2) \\ 1.714(2) \\ 1.703 \end{array}$ | 1.632(2) 1.614(2) 1.623 | $\begin{array}{c} 1.623(2) \\ 1.622(2) \\ 1.629(2) \\ 1.598(2) \\ 1.618 \end{array}$ |
| 37BAV | 2.608(2) 2.343(2) 2.456(2) 2.546(2) 2.341(2) 2.462(2) 2.452(2) | $1.654(2) \\ 1.617(2) \\ 1.636$ | $\begin{array}{c} 1.638(3) \\ 1.626(5) \\ 1.693(5) \\ 1.649 \end{array}$ | $\begin{array}{c} 1.695(3) \\ 1.578(3) \\ 1.614(2) \\ 1.625 \end{array}$ | 1.696(2) 1.722(2) 1.709 | $\begin{array}{c} 1.626(2) \\ 1.612(2) \\ 1.619 \end{array}$ | $\begin{array}{c} 1.623(2) \\ 1.623(2) \\ 1.623(2) \\ 1.628(2) \\ 1.597(2) \\ 1.618 \end{array}$ |
| 36ABAV | 2.615(2) 2.345(2) 2.457(3) 2.532(3) 2.532(3) 2.336(2) 2.461(2) 2.451 | $1.656(4) \\ 1.616(3) \\ 1.636$ | $\begin{array}{c} 1.632(4) \\ 1.627(7) \\ 1.684(7) \\ 1.644 \end{array}$ | $\begin{array}{c} 1.691(4) \\ 1.579(4) \\ 1.612(3) \\ 1.624 \end{array}$ | $1.697(3) \\ 1.720(3) \\ 1.709$ | $1.634(3) \\ 1.613(2) \\ 1.624$ | $\begin{array}{c} 1.622(3)\\ 1.623(3)\\ 1.629(3)\\ 1.600(2)\\ 1.619\end{array}$ |
| 35BAV | 2.523(4) 2.375(3) 2.429(4) 2.638(4) 2.638(4) 2.355(4) 2.355(4) 2.352(4) 2.453(4) 2.453(4) | $\begin{array}{c} 1.659(6) \\ 1.623(6) \\ 1.641 \end{array}$ | 1.632(7) 1.643(13) 1.672(12) 1.645 | $\begin{array}{c} 1.697(7) \\ 1.573(7) \\ 1.628(5) \\ 1.632 \end{array}$ | $\begin{array}{c} 1.633(4) \\ 1.676(3) \\ 1.655 \end{array}$ | 1.634(4) 1.599(4) 1.617 | $\begin{array}{c} 1.629(4) \\ 1.619(4) \\ 1.637(4) \\ 1.595(4) \\ 1.620 \end{array}$ |
| 33BAV | $\begin{array}{c} 2.628(2)\\ 2.340(1)\\ 2.457(2)\\ 2.512(2)\\ 2.512(2)\\ 2.334(2)\\ 2.414(2)\\ 2.462(1)\\ 2.450\end{array}$ | $\begin{array}{c} 1.659(2) \\ 1.616(2) \\ 1.638 \end{array}$ | $\begin{array}{c} 1.629(3) \\ 1.631(4) \\ 1.688(4) \\ 1.644 \end{array}$ | $\begin{array}{c} 1.690(2) \\ 1.570(2) \\ 1.604(2) \\ 1.617 \end{array}$ | 1.716(2) 1.737(2) 1.727 | $\begin{array}{c} 1.625(2) \\ 1.614(2) \\ 1.620 \end{array}$ | $\begin{array}{c} 1.622(2)\\ 1.621(2)\\ 1.631(2)\\ 1.600(2)\\ 1.619\end{array}$ |
| 32BAV | 2.559(2) 2.361(2) 2.438(2) 2.584(2) 2.342(2) 2.342(2) 2.342(2) 2.454(2) 2.454(2) | $\begin{array}{c} 1.650(3) \\ 1.623(2) \\ 1.637 \end{array}$ | $\begin{array}{c} 1.631(3)\\ 1.628(5)\\ 1.683(5)\\ 1.683(5)\\ 1.643\end{array}$ | $\begin{array}{c} 1.689(2) \\ 1.569(3) \\ 1.624(2) \\ 1.627 \end{array}$ | $\begin{array}{c} 1.650(2) \\ 1.685(2) \\ 1.668 \end{array}$ | $\begin{array}{c} 1.638(2) \\ 1.610(2) \\ 1.624 \end{array}$ | $\begin{array}{c} 1.621(2)\\ 1.622(2)\\ 1.630(2)\\ 1.595(2)\\ 1.617\end{array}$ |
| 31BAV | 2.610(2) 2.346(2) 2.455(2) 2.537(2) 2.338(2) 2.410(2) 2.462(2) 2.451 | $\begin{array}{c} 1.655(3) \\ 1.617(3) \\ 1.636 \end{array}$ | $\begin{array}{c} 1.631(3)\\ 1.634(5)\\ 1.688(5)\\ 1.646\end{array}$ | $\begin{array}{c} 1.694(3) \\ 1.573(3) \\ 1.611(2) \\ 1.622 \end{array}$ | 1.698(2) 1.722(2) 1.710 | $\begin{array}{c} 1.628(2) \\ 1.612(2) \\ 1.620 \end{array}$ | $\begin{array}{c} 1.624(2)\\ 1.622(2)\\ 1.632(2)\\ 1.632(2)\\ 1.597(2)\\ 1.619\end{array}$ |
| 29BAV | $\begin{array}{c} 2.603(1)\\ 2.349(1)\\ 2.453(1)\\ 2.539(1)\\ 2.539(1)\\ 2.335(1)\\ 2.460(1)\\ 2.450\end{array}$ | $\begin{array}{c} 1.657(2) \\ 1.619(2) \\ 1.638 \end{array}$ | $\begin{array}{c} 1.631(2) \\ 1.632(4) \\ 1.689(4) \\ 1.646 \end{array}$ | $\begin{array}{c} 1.692(2) \\ 1.568(2) \\ 1.613(1) \\ 1.612 \end{array}$ | 1.689(1) 1.713(1) 1.701 | $\begin{array}{c} 1.634(1) \\ 1.613(1) \\ 1.624 \end{array}$ | $\begin{array}{c} 1.622(1)\\ 1.621(1)\\ 1.632(1)\\ 1.632(1)\\ 1.600(1)\\ 1.619\end{array}$ |
| 28BAV | $\begin{array}{c} 2.628(1)\\ 2.339(1)\\ 2.457(2)\\ 2.519(2)\\ 2.519(2)\\ 2.337(2)\\ 2.415(1)\\ 2.455(1)\\ 2.451\\ \end{array}$ | $\begin{array}{c} 1.654(2) \\ 1.617(2) \\ 1.636 \end{array}$ | $\begin{array}{c} 1.633(3)\\ 1.634(4)\\ 1.689(4)\\ 1.647\end{array}$ | $\begin{array}{c} 1.695(2) \\ 1.574(2) \\ 1.608(1) \\ 1.621 \end{array}$ | 1.716(2) 1.734(2) 1.725 | $\begin{array}{c} 1.626(1) \\ 1.612(1) \\ 1.619 \end{array}$ | $\begin{array}{c} 1.625(2)\\ 1.622(2)\\ 1.630(2)\\ 1.598(2)\\ 1.619\end{array}$ |
| 27BAV | 2.632(1) 2.338(1) 2.460(1) 2.511(1) 2.511(1) 2.334(1) 2.464(1) 2.451 | $\begin{array}{c} 1.661(2) \\ 1.616(2) \\ 1.639 \end{array}$ | $\begin{array}{c} 1.629(2) \\ 1.637(3) \\ 1.691(3) \\ 1.647 \end{array}$ | 1.692(2) 1.576(2) 1.607(1) 1.621 | $\begin{array}{c} 1.720(1) \\ 1.740(1) \\ 1.730 \end{array}$ | 1.627(1) 1.612(1) 1.620 | $\begin{array}{c} 1.622(1)\\ 1.624(1)\\ 1.631(1)\\ 1.601(1)\\ 1.620\end{array}$ |
| | | 0 7 X | × 2 | × 2 | 2 7 2 2 | $\times 2 \times 2 \times 2$ | |
| | $\begin{array}{c} Ca - 0(1) \\ Ca - 0(2) \\ Ca - 0(3) \\ Ca - 0(3) \\ Ca - 0(4) \\ Ca - 0(7) \\ Ca - 0(8) \\ Ca - 0(9) \\ < Ca - 0 \\ \end{array}$ | T(1)-O(1) T(1)-O(9) < T(1)-O> | T(2)-O(7) T(2)-O(8) T(2)-O(9) < T(2)-O> | T(3)-O(1) T(3)-O(2) T(3)-O(3) < T(3)-O> | T(4)-O(3) T(4)-O(4) < T(4)-O> | T(5) - O(4) T(5) - O(5) < T(5) - O> | T(6)-O(5) T(6)-O(6) T(6)-O(6) T(6)-O(7) < T(6)-O> |

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| | <i>T</i> | (3) | <i>T</i> | (4) |
|---------------|----------|---------|----------|---------|
| | EMPA | SREF | EMPA | SREF |
| 2ABAV | 19.9 | 21.2(2) | 26.8 | 26.0(1) |
| 7BAV | 19.2 | 19.5(1) | 26.9 | 26.7(1) |
| 10BAV | 22.0 | 23.0(2) | 26.6 | 26.1(1) |
| 11BAV | 18.0 | 18.7(1) | 26.9 | 26.7(1) |
| 12BAV | 15.0 | 16.7(2) | 27.4 | 27.0(2) |
| 13BAV | 23.1 | 24.3(2) | 26.5 | 26.3(1) |
| 14BAV | 17.2 | 18.0(2) | 27.1 | 26.1(1) |
| 15BAV | 26.2 | 26.5(1) | 26.1 | 26.3(1) |
| 19BAV | 25.4 | 25.3(1) | 26.3 | 26.3(1) |
| 21BAV | 25.8 | 25.4(2) | 26.2 | 26.4(1) |
| 23BAV | 21.0 | 20.7(3) | 26.7 | 26.3(2) |
| 25BAV | 25.2 | 24.4(1) | 26.3 | 26.4(1) |
| 27BAV | 26.7 | 26.4(1) | 26.2 | 26.3(1) |
| 28BAV | 26.5 | 25.7(1) | 26.1 | 26.3(1) |
| 29BAV | 23.4 | 23.5(1) | 26.5 | 26.1(1) |
| 31BAV | 23.7 | 24.1(2) | 26.4 | 26.1(1) |
| 32BAV | 19.1 | 19.0(2) | 26.9 | 26.9(1) |
| 33BAV | 24.3 | 25.7(1) | 26.3 | 26.2(1) |
| 35BAV | 14.4 | 16.8(4) | 27.4 | 26.9(2) |
| 36ABAV | 25.0 | 24.3(3) | 26.3 | 26.3(2) |
| 37BAV | 22.2 | 24.2(2) | 26.6 | 26.3(1) |
| 39BAV | 21.3 | 24.0(1) | 26.6 | 25.9(1) |
| 40BAV | 18.6 | 18.2(2) | 27.0 | 26.9(1) |
| 41BAV | 23.0 | 23.3(4) | 26.5 | 26.6(3) |
| <dev.></dev.> | 0 | .9 | 0 | .3 |

TABLE 6. Site-scattering values (e.p.f.u.) for bavenite derived from SREF and EMPA.

be used to examine short-range (i.e. nonaveraged) arrangements in a structure (Hawthorne et al., 1996a, 2006). Table 7 gives the (average) bond-valence arrangements for a high-Be structure (14BAV) and a low-Be structure (27BAV). We can derive probable bond-valences for ordered arrangements by scaling the bond-valences to sum to the ideal incident sums dictated by the valence-sum rule. Thus for the composition Ca₄Be₂Si₇O₂₄(OH)₂ [Si₂Al₂O₂], we scale the bond valences involving the T(3) and T(4) sites in the low-Be crystal (27BAV) to sum to 4.00 (= Si) and 3.00 v.u. (= Al), respectively, and obtain the bond valences for local (real, not averaged) arrangements of Si and Al that incorporate the effects of strain (at other cations and anions) that are present in the averaged structure (Table 8a). Similarly, for the composition Ca₄Be₂Si₇O₂₄(OH)₂[Be₂Si₂(OH)₂], we scale the bond valences involving the T(3)and T(4) sites in the high-Be crystal (14BAV) to sum to 3.00 (= Be) and 4.00 v.u. (= Si),

respectively (Table 8*b*). These values may be used for arguments involving short-range order and local structure.

Constraints involving the (OH) anions

The environments of the O(8) and O(2) sites are illustrated in Figs 6 and 7. Excluding H, the O(8) anion is bonded to atoms at the Ca ($\times 2$) and T(2) sites. The T(2) site is occupied only by Be and the *Ca* site is dominantly occupied by Ca with very minor to trace Na (we will ignore Na in this discussion as it averages 0.02 a.p.f.u. in our samples, except for 35BAV which has 0.145 a.p.f.u. Na). Thus, the nearest-neighbour cations to O(8) will be dominated by Ca and Be: $^{T(2)}$ Be–Ca–Ca–O(8). The T(2) tetrahedron links only to the T(6) tetrahedron and the Ca polyhedron. As the T(6) site is occupied only by Si, the next-nearest-neighbour sites show no chemical variation and hence no possibilities for different short-range arrangements.

CHEMICAL AND STRUCTURAL VARIATIONS IN BAVENITE

| | Ca | <i>T</i> (1) | <i>T</i> (2) | <i>T</i> (3) | <i>T</i> (4) | <i>T</i> (5) | <i>T</i> (6) | Σ |
|------------------|---|-----------------------------|--------------|-------------------------------------|-----------------------------|--------------|---|--------------|
| O(1) | $0.21^{\times 2 \rightarrow}$ | $0.93^{\times 2\downarrow}$ | | 0.62 | | | | 1.96 |
| O(2) O(3) | 0.34 0.28 | | | 0.87 $0.74^{\times 2\downarrow}$ | 0.99 ^{×2↓} | | | 2.01 |
| O(4) | 0.19 | | | | $0.89^{\times 2\downarrow}$ | 0.96 ×2↓ | | 2.04 |
| O(5) O(6) | | | | | | 1.04 | $\begin{array}{c} 1.00 \\ 0.99 \end{array} \times 2 \downarrow \rightarrow \end{array}$ | 2.05 1.98 |
| O(7) | 0.36 | | 0.51 × 2↓ | | | | 1.07 | 1.95 |
| O(8) O(9) | $\begin{array}{c} 0.31^{\times2} \\ 0.27^{\times2} \end{array}$ | $1.01^{\times 2\downarrow}$ | 0.51 0.44 | | | | | 1.14 1.98 |
| Σ EMPA | 1.97 2.00 | 3.87 4.00 | 1.97 2.00 | 2.97 2.92 | 3.78 3.54 | 4.00 4.00 | 4.06 4.00 | |

TABLE 7*a*. Bond-valence calculations for a high-Be (14BAV) bavenite sample.

Table 7b. Bond valence calculations for a low-Be (27BAV) bavenite sample.

| | Ca | T(1) | <i>T</i> (2) | <i>T</i> (3) | T(4) | <i>T</i> (5) | <i>T</i> (6) | Σ |
|------|-------------------------------|-----------------------------|---------------------|----------------------|-----------------------------|--------------|---------------------------------------|------|
| O(1) | 0.16 ^{×2→} | 0.90 ^{×2↓} | | 0.81 | | | | 2.04 |
| O(2) | $0.36^{\times 2 \rightarrow}$ | | | 1.10 | | | | 1.82 |
| O(3) | 0.26 | | | 1.01 ^{× 2↓} | $0.82^{\times 2\downarrow}$ | | | 2.10 |
| O(4) | 0.23 | | | | $0.78^{\times 2\downarrow}$ | 0.99 ×2↓ | | 2.00 |
| 0(5) | | | | | | 1.03 ×2↓ | 1.01 | 2.04 |
| 0(6) | | | | | | | $0.99 \times 2\downarrow \rightarrow$ | 1.97 |
| O(7) | 0.36 | | 0.51 ^{×2↓} | | | | 1.06 | 1.94 |
| O(8) | $0.29^{\times 2 \rightarrow}$ | | 0.50 | | | | | 1.08 |
| O(9) | $0.26^{\times 2 \rightarrow}$ | $1.02^{\times 2\downarrow}$ | 0.43 | | | | | 1.97 |
| Σ | 1.92 | 3.85 | 1.96 | 3.94 | 3.21 | 4.05 | 4.05 | |
| EMPA | 1.96 | 4.00 | 2.00 | 3.87 | 3.10 | 4.00 | 4.00 | |

Excluding H, the O(2) anion is bonded to atoms at the Ca (\times 2) and T(3) sites. The T(3) site is occupied by Si and Be and the nearest-neighbour cations will be dominated by Si, Be and Ca; the algebraically possible short-range arrangements are as follows: T(3)Si-Ca-Ca-O(2) and T(3)Be-Ca-Ca-O(2). The occupancy of the O(2) site in these local arrangements is controlled by the bond valence incident at the O(2) site. Inspection of Table 8 shows incident bond-valence sums of 2.06 and 1.27 v.u. for the clusters ^{T(3)}Si-Ca-Ca-O(2) and $T^{(3)}Be-Ca-Ca-O(2)$. Hence the O(2) site is occupied by (OH) where T(3) is locally occupied by Be (Table 8a) and is occupied by O^{2-} where T(3) is locally occupied by Si (Table 8b). Hence there is only one crystalchemically possible local cluster around the O(2) site where O(2) = (OH): ^{T(3)}Be-Ca-Ca-O(2).

Possible order involving the T(3)-T(4)-T(3)-T(4) ring

A prominent linkage in the structure of bavenite is the four-membered T(3)-T(4)-T(3)-T(4) ring that may be seen (coloured rose and green) in Fig. 1. The T(3) site may be occupied by Si and Be, and the T(4) site may be occupied by Al and Si. There are nine algebraically possible distinct ring compositions; these are listed in Table 9. The bridging anion in the T(3)-T(4)-T(3)-T(4) ring is O(3); do the bond-valence requirements of the O(3) anion exert any constraints on the possible cation arrangements in the T(3)-T(4)-T(3)-T(4)ring? The O(3) anion is coordinated by the T(3), T(4), Ca and H(2) cations, and the possible local cation arrangements are as follows: ^{T(3)}Be- $T^{(4)}$ Si-Ca-H(2), $T^{(3)}$ Be $-T^{(4)}$ Al-Ca-H(2), $T^{(3)}Si^{-T^{(4)}}Al^{-Ca}-H^{(2)}$ and $T^{(3)}Si^{-T^{(4)}}Si^{-$ Ca-H(2), where the H(2) site may be occupied

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FIG. 2. The crystal structure of bavenite projected onto (001). Legend as in Fig. 1, Ca sites are shown by blue circles, Ca-O bonds are shown by red lines.

by H or \square (vacancy) depending on the local occupancy of the T(3) site in the adjacent T(3)-T(4)-T(3)-T(4) ring. This point is illustrated in Fig. 10. The O(3) anion in the



FIG. 3. Variation in Be content derived by SREF as a function of Be content derived by stoichiometric calculation from the electron microprobe analyses

(EMPA); the line shows the 1:1 relation.

T(3)-T(4)-T(3)-T(4) ring to the right receives a hydrogen bond from a donor O(2) anion in the adjacent T(3)-T(4)-T(3)-T(4) ring. This is an important point because it means that the arrangements $T^{(3)}Si^{-T(4)}Al-Ca-H(2)$ and



FIG. 4. Variation in $\langle T(4) - O \rangle$ as a function of Al in bayenite structures; the bars show ± 1 standard deviation.



FIG. 5. Variation in $^{T(4)}$ Al as a function of $^{T(3)}$ Be in bavenite; the line shows the relation $^{T(4)}$ Al + $^{T(3)}$ Be = 2.0 a.p.f.u.

^{*T*(3)}Si-^{*T*(4)}Si-Ca-H(2) can have the H(2) site occupied by H (even though the local T(3) site is occupied by Si) because it is the composition of the adjacent ring that affects occupancy of H(2). From Tables 8*a* and 8*b*, the magnitudes of the local bond-valences to O(3) are approximately as follows: ^{*T*(3)}Be-O(3) = 0.50, ^{*T*(3)}Si-O(3) = 1.03, ^{*T*(4)}Si-O(3) = 1.05, ^{*T*(4)}Al-O(3) = 0.77, Ca-O(3) = 0.27 and H(2) \approx 0.27 or 0.00 v.u. The bond-valence sums around O(3) for each of these local arrangements are shown in Table 10. These calculations indicate that the arrangements ^{*T*(3)}Si-^{*T*(4)}Si-Ca-H (sum = 2.61 v.u.) and



FIG. 6. The hydrogen-bond arrangement around the O(8) anion in bavenite; legend as in Fig. 1, the H atom is shown by a small red circle and hydrogen bonds are shown as black dashed lines.



FIG. 7. The hydrogen-bond arrangement around the O(2) anion in bavenite; legend as in Fig. 6, other short O(donor)–O distances are shown by dotted lines.

^{*T*(3)}Be^{-T(4)}Al–Ca– \Box (sum = 1.55 v.u.) cannot occur. The arrangements ^{*T*(3)}Si–^{*T*(4)}Si–Ca– \Box and ^{*T*(3)}Si–^{*T*(4)}Al–Ca–H have bond-valence sums of 2.35 v.u., which suggests that these also should not occur. However, the bulk composition of these minerals conforms to the constraint ^{*T*(3)}Be = ^{*T*(4)}Si. As a result of this, if ^{*T*(3)}Si–O(3)–^{*T*(4)}Si linkages are not possible, then only ^{*T*(3)}Be–O(3)–^{*T*(4)}Si and ^{*T*(3)}Si–O(3)–^{*T*(4)}Al linkages can occur, and there will be no



FIG. 8. Variation in ^{SREF}Be content as a function of the *b* cell-dimension in bavenite. The data follow a linear relation (full line) which extrapolates (dashed line) to a Be content of 4 a.p.f.u. at $b \approx 4.918$ Å. The horizontal line shows the maximum extent of the bavenite series proposed by Beus (1966).

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| | Са | <i>T</i> (1) | <i>T</i> (2) | T(3) = Be | $T(4) = \mathrm{Si}$ | <i>T</i> (5) | <i>T</i> (6) | Σ | H(2) | H(8) | Σ |
|------|-----------------------------|----------------------|--------------|---------------|----------------------|--------------|-----------------------------|------------------|-------|------|------|
| 0(1) | $0.21 \times 2 \rightarrow$ | 0.93 ×2↓ | | 0.41 | | | | 1.76 | | | 1.76 |
| O(2) | 0.34 ×2→ | | | 0.59 | | | | 1.27 | 0.73 | | 2.00 |
| O(3) | 0.28 | | | 0.50 ×2↓ | 1.05 ×2↓ | | | 1.83 | 0.27 | | 2.10 |
| O(4) | 0.19 | | | | 0.95 ×2↓ | 0.96 ×2↓ | | 2.10 | | | 2.10 |
| O(5) | | | | | | 1.04 ×2↓ | 1.00 | 2.04 | | | 2.04 |
| O(6) | | | | | | | $0.99 \times 2 \rightarrow$ | 1.98 | | 0.07 | 2.05 |
| O(7) | 0.36 | | 0.51 ×2↓ | | | | 1.07 | 1.94 | | | 1.94 |
| O(8) | $0.31 \times 2 \rightarrow$ | | 0.51 | | | | | 1.13 | | 0.93 | 2.06 |
| O(9) | $0.27 \times 2 \rightarrow$ | 1.01 ×2↓ | 0.44 | | | | | 1.99 | | | 1.99 |
| Σ | 1.97 | 3.87 | 1.97 | 2.00 | 4.00 | 4.00 | 4.06 | | 1.00 | 1.00 | |
| | Tab | ole 8 <i>b</i> . Bon | d-valence | table for she | ort-range ar | rangement | ts: $T(3) = Si$ | , <i>T</i> (4) = | = Al. | | |
| | Ca | <i>T</i> (1) | <i>T</i> (2) | T(3) =Si | T(4) = Al | <i>T</i> (5) | <i>T</i> (6) | Σ | H(2) | H(8) | Σ |

TABLE 8*a*. Bond-valence table for short-range arrangements: T(3) = Be, T(4) = Si.

| | Ca | I(1) | I(2) | 1(3) = 51 | I(4) = AI | I(5) | I(0) | L | H(2) | H(8) | Z |
|------|-----------------------------|----------|---------------------|-----------|-----------|----------|-----------------------------|------|------|------|------|
| O(1) | 0.16 ×2→ | 0.90 ×2↓ | | 0.82 | | | | 2.04 | | | 2.04 |
| O(2) | $0.36 \times 2 \rightarrow$ | | | 1.12 | | | | 1.84 | | | 1.84 |
| O(3) | 0.26 | | | 1.03 ×2↓ | 0.77 ×2↓ | | | 2.06 | | | 2.06 |
| O(4) | 0.23 | | | | 0.73 ×2↓ | 0.99 ×2↓ | | 1.95 | | | 1.95 |
| O(5) | | | | | | 1.03 ×2↓ | 1.01 | 2.04 | | | 2.04 |
| O(6) | | | | | | | $0.99 \times 2 \rightarrow$ | 1.98 | | 0.05 | 2.03 |
| O(7) | 0.36 | | 0.51 ^{×2↓} | | | | 1.06 | 1.93 | | | 1.93 |
| O(8) | $0.29 \times 2 \rightarrow$ | | 0.50 | | | | | 1.08 | | 0.95 | 2.03 |
| O(9) | $0.26 \times 2 \rightarrow$ | 1.02 ×2↓ | 0.43 | | | | | 1.97 | | | 1.97 |
| Σ | 1.92 | 3.85 | 1.96 | 4.00 | 3.00 | 4.04 | 4.06 | | | 1.00 | |
| | | | | | | | | | | | |

 $^{T(3)}$ Be-O(3)- $^{T(4)}$ Al linkages. The occurrence of these local arrangements can be tested by 27 Al MAS NMR as Al occurs only at T(4) and the resultant band(s) will represent only local environments around the T(4) site. If there are

no $^{T(3)}$ Si-O(3)- $^{T(4)}$ Si linkages, then there is only one local next-nearest-neighbour arrangement involving Al at T(4): $^{T(3)}$ Si- $^{T(4)}$ Al- $^{T(3)}$ Si. If there are $^{T(3)}$ Si-O(3)- $^{T(4)}$ Si linkages, then there are three local next-nearest-neighbour arrangement involving Al at T(4): $^{T(3)}$ Be- $^{T(4)}$ Al- $^{T(3)}$ Be, $^{T(3)}$ Si- $^{T(4)}$ Al- $^{T(3)}$ Be and $^{T(3)}$ Si- $^{T(4)}$ Al- $^{T(3)}$ Si.



FIG. 9. Variation in Na content as a function of Ca content in bavenite; the black circles denote bavenites with Be > 3 a.p.f.u.

TABLE 9. All possible T(3)-T(4)-T(3)-T(4) configurations.

| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | | | | |
|--|------|--------------|--------------|--------------|--------------|
| IBeSiBeSiIIBeSiBeAlIIIBeAlBeAlIVBeSiSiSiVBeSiSiAlVIBeAlSiAlVIISiSiSiSiVIIISiSiSiAlIXSiAlSiAl | | <i>T</i> (3) | <i>T</i> (4) | <i>T</i> (3) | <i>T</i> (4) |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | Ι | Be | Si | Be | Si |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | II | Be | Si | Be | Al |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | III | Be | Al | Be | Al |
| VBeSiSiAlVIBeAlSiAlVIISiSiSiSiVIIISiSiSiAlIXSiAlSiAl | IV | Be | Si | Si | Si |
| VIBeAlSiAlVIISiSiSiSiVIIISiSiSiAlIXSiAlSiAl | V | Be | Si | Si | Al |
| VIISiSiSiSiVIIISiSiSiAlIXSiAlSiAl | VI | Be | Al | Si | Al |
| VIII Si Si Si Al IX Si Al Si Al | VII | Si | Si | Si | Si |
| IX Si Al Si Al | VIII | Si | Si | Si | Al |
| | IX | Si | Al | Si | Al |

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FIG. 10. An oblique view of adjacent T(3)-T(4)-T(3)-T(4) rings in the bavenite structure. The O(3) anion in one ring receives a hydrogen bond from the donor O(2) anion in the adjacent ring. Legend as in Fig. 2.

Figure 11 shows ²⁷Al MAS NMR spectra for samples 40BAV and 41BAV. In each sample,



FIG. 11. ²⁷Al MAS NMR spectra for bavenites 40BAV and 41BAV; the three distinct bands are labelled A, B and C, and occur at 60, 51 and 38 ppm, respectively.

there is one maximum but the overall envelope also shows two distinct shoulders, three bands in all, labelled A, B and C in Fig. 11, indicating three distinct short-range arrangements around Al at T(4). Thus the ²⁷Al MAS NMR spectra (Fig. 11) force us to conclude that $^{T(3)}Si-O(3)-^{T(4)}Si$ linkages are possible, and hence the arrangement $^{T(3)}Si-^{T(4)}Si-Ca-\Box$ can occur. Moreover, the similarity in local incident bond-valence sums around O(3) for the arrangements $^{T(3)}Si-^{T(4)}Si-Ca-\Box$ and $^{T(3)}Si-^{T(4)}Al- Ca-H$ suggests that the latter also can occur. Presumably there can be sufficient local relaxation of bondlengths to adjust to these arrangements.

FTIR spectroscopy

Fourier-transform infrared spectroscopy is sensitive to short-range order and has been used extensively to probe short-range order in complex solid-solutions (e.g. Hawthorne *et al.*, 1996b, 2000, 2005, 2007; Della Ventura *et al.*, 1996, 1998, 1999, 2007). Above, we argue that particular short-range arrangements should occur in bavenite. The FTIR spectra of four bavenite samples, 25BAV, 32BAV, 40BAV and 41BAV, are shown in Fig. 12. There are two principal maxima at ~3625 and ~3545 cm⁻¹. The envelope of the maximum at ~3545 cm⁻¹ has inflection points indicative of fine structure, and five sets of constituent bands (labelled A to E in Fig. 12) can be identified in the four spectra. There are two crystallographically



FIG. 12. FTIR spectra for selected bavenites in the principal (OH)-stretching region; data are shown as hollow squares.

distinct OH groups in the bavenite structure, O(8)(Fig. 6) and O(2) (Fig. 7), and the presence of more than two bands in the principal (OH)-stretching region is indicative of the presence of distinct short-range ordered arrangements around one or both of the O(8) and O(2) sites.

Above, we proposed one short-range arrangement around the O(8) site: T(2)Be-Ca-Ca-O(8)=(OH), and we expect one peak in the IR from this arrangement. For the O(2) site, only arrangements that involve (OH) at O(2) give signals in the IR, and there is one such nearestneighbour arrangement: T(3)Be-Ca-Ca-O(2)=(OH). The O(3) anion bridges between the T(3) and T(4) tetrahedra and has four nearestneighbour arrangements: $T^{(3)}Si^{-T^{(4)}}Si$, $^{T(3)}$ Si^{- $^{T(4)}$}Al, $^{T(3)}$ Be^{- $^{T(4)}$}Si and $^{T(3)}$ Be^{- $^{T(4)}$}Al. As a result, the bond valences incident at O(3) from these different nearest-neighbour arrangements will be different from each other, and the strengths of the resulting hydrogen bonds will be different, shifting the absorption frequency for each arrangement (and producing a concomitant relaxation around the O(2) anion as required by the valence-sum rule). Thus we expect four peaks in the IR from the arrangement ⁷⁽³⁾Be-Ca-Ca-O(2)=(OH) due to the four next-nearest-neighbour arrangements around the acceptor O(3) anion in the adjacent T(3)-T(4)-T(3)-T(4) ring: $^{T(3)}$ Be $^{-T(4)}$ Si (arrangements 1 and 2, Table 10), $^{T(3)}$ Be $^{-T(4)}$ Al (arrangement 3), $^{T(3)}$ Si $^{-T(4)}$ Al (arrangements 5 and 6), and $^{T(3)}Si^{-T(4)}Si$ (arrangement 8). We now need to assign these arrangements to the bands fitted to the spectra in Fig. 12.

The cluster $^{T(2)}$ Be–Ca–Ca–O(8)=(OH) is present in the same amount in each sample, and shows no local variation around the H(8) atom that could give rise to fine structure, whereas the

TABLE 10. Scaled bond-valence sums at O(3) for all possible configurations from Table 9.

| | <i>T</i> (3) | <i>T</i> (4) | Са | H(2) | T(3) - O(3) | <i>T</i> (4)–O(3) | Ca-O(3) | HO(3) | Σ (v.u.) | Possible |
|---|--------------|--------------|----|------|-------------|-------------------|---------|-------|-------------|----------|
| 1 | Be | Si | Ca | Н | 0.5 | 1.03 | 0.28 | 0.27 | 2.08 | Yes |
| 2 | Be | Si | Ca | | 0.5 | 1.03 | 0.28 | 0 | 1.81 | Yes |
| 3 | Be | Al | Ca | H | 0.5 | 0.77 | 0.28 | 0.27 | 1.82 | Yes |
| 4 | Be | Al | Ca | | 0.5 | 0.77 | 0.28 | 0 | 1.55 | No |
| 5 | Si | Al | Ca | H | 1.03 | 0.77 | 0.28 | 0.27 | 2.35 | Yes |
| 6 | Si | Al | Ca | | 1.03 | 0.77 | 0.28 | 0 | 2.08 | Yes |
| 7 | Si | Si | Ca | H | 1.03 | 1.03 | 0.28 | 0.27 | 2.61 | No |
| 8 | Si | Si | Ca | | 1.03 | 1.03 | 0.28 | 0 | 2.34 | Yes |



FIG. 13. Incident bond-valence at O(2) vs. $^{T(3)}$ Be a.p.f.u. for all bavenite samples. The ideal curve passes through 1.2 and 2.0 v.u. at the O(2) anion for $^{T(3)}$ Be = 2 a.p.f.u. and unprotonated $^{T(3)}$ Be = 0 a.p.f.u., respectively.

H(2) atom shows four different local arrangements of nearest- and next-nearest-neighbour cations that should give rise to four stretching bands in the infrared. The spectra (Fig. 12) show a single symmetrical band at $\sim 3635 \text{ cm}^{-1}$ and a four-band envelope centred at ~3545 cm⁻¹. Accordingly, we assign the band at \sim 3635 cm⁻¹ (labelled A in Fig. 12) to the ^{T(2)}Be-Ca-Ca-O(8)=(OH) cluster and the envelope centred at ~3545 cm⁻¹ to bands involving the $T^{(3)}$ Be–Ca– Ca-O(2)=(OH) cluster (and labelled B-E in Fig. 12). Note that the amount of (OH) at the O(8) site (2 a.p.f.u., Table 3) is always in excess of the amount of (OH) at the O(2) site (<2 a.p.f.u., Table 3) and yet the relative intensity of band A [assigned to (OH) at O(8)] is considerably less than the relative intensity of the envelope of bands B-E assigned to (OH) at O(2) (Fig. 12). This is a result of the fact that the transition moment is an inverse function of the energy of the transition (where coupling of adjacent arrangements does not occur) (Skogby and Rossman, 1991; Burns and Hawthorne, 1994; Groat *et al.*, 1995).

Assignment of the B-E bands may be done by examining the relative strengths of the hydrogen bonds to O(3) required by the valence-sum rule. Where O(3) bridges the $T^{(3)}Si^{-T(4)}Si$ arrangement, the O(3) anion requires very little bond-valence from H(2), the associated O-H stretching frequency will be high, and band B may be assigned to this arrangement. Similarly, the bands C, D and E may be assigned to the local arrangements associated with increasing hydrogen-bond-valences: $T^{(3)}Si^{-T^{(4)}}Al$, $T^{(3)}Be^{-T^{(4)}}Si$ and $T^{(3)}Be^{-T^{(4)}}Al$, respectively. This local effect has a strong influence on the longrange aspects of the structure around the O(2) site. This is shown by the variation in the calculated bond-valence sum at O(2) as a function of the (calculated) $T^{(3)}$ Be content for all samples (Fig. 13). Assuming an average Odonor-H bondvalence of ~0.8 v.u., the incident bond-valence at O(2) should vary linearly between the points $(\Sigma BVO(2) = 2.0, T^{(3)}Be = 0.0)$ where no H is present at O(2) and ($\Sigma BVO(2) = 1.2$, $T^{(3)}Be = 2.0$) where only (OH) is present at O(2). Although the data are broadly in accord with the model of SRO presented above, they do deviate systematically from the ideal relation (shown as the full line in Fig. 13). The data extrapolate to an incident bondvalence sum of ~1.9 v.u. for $^{T(3)}Be = 0.0$ a.p.f.u., indicating that the structure has significant strain



FIG. 14. The linkage of two T(3)-T(4)-T(3)-T(4) rings along the **c** direction through the T(1) tetrahedron projected onto (010); note that the T(1) (= Si) tetrahedron links to two T(2) (= Be) tetrahedra and two T(3) (= Be and/or Si) tetrahedra.

around O(2) at this value, and that this local strain decreases with increasing Be and becomes zero at $^{T(3)}$ Be = 1.0 a.p.f.u.

Short-range order controls the limits of $^{T(3)}Be \rightleftharpoons ^{T(3)}Si$ substitution

As noted above, there are two end-members involved in the bavenite solid-solution series: $Ca_4Be_2Si_7O_{24}(OH)_2[Be_2Si_2(OH)_2]$ and $Ca_4Be_2Si_7O_{24}(OH)_2[Si_2Al_2O_2]$. The compositions given here (Table 3, Fig. 8) span this range and do not extend much past the middle of the series toward the composition $Ca_4Be_2Si_7O_{24}(OH)_2$ [Be₂Si₂(OH)₂], in accord with the proposal of Beus (1966). What is the constraint that does not allow compositions in the second half of the compositional range?

The substitution $^{T(4)}Si + ^{T(3)}Be + ^{O(2)}OH^{-} \rightleftharpoons ^{T(4)}Al + ^{T(3)}Si + ^{O(2)}O^{2-}$ involves the T(3) and T(4) tetrahedra. As shown in Fig. 1, these tetrahedra form a four-membered ring in the sequence T(3)-T(4)-T(3)-T(4). Figure 14 shows the linkage of these rings in the c direction through the T(1) (= Si) tetrahedron via the T(3)tetrahedra of adjacent rings. Let us examine the short-range bond-valence distribution where one of the T(3) tetrahedra is occupied by Be, and the other by a cation that gives a T(3)-O(1) bondvalence of X v.u., taking the relevant values from Table 8. The sum of the bond valence incident at the T(1) tetrahedron is as follows: $0.44 \times$ $2 [T(2)-O(9) \times 2] + 0.27 \times 4 [Ca-O(9) \times 4] +$ $0.41 \times 1 [T(3) - O(1), T(3) = Be] + 0.21 \times$ $4 [Ca-O(1) \times 4] + X [T(3)-O(1), T(3) = not$ specified] = (3.21 + X) v.u. As T(1) = Si, the valence-sum rule requires that the bond-valence incident at the T(1) tetrahedron is 4 v.u., and hence X = 0.79 v.u. Inspection of the local bondvalence arrangement where T(3) = Si (Table 8b) shows that T(3) - O(1) has a bond valence of 0.82 v.u., close to the value of 0.79 v.u. required for satisfaction of the bond-valence requirements of the T(1) tetrahedron where T(1) links to Be at one of the two adjacent T(3) sites. Thus, where $T^{(3)}$ Be participates in the linkage $T^{(3)}-T^{(1)}-T^{(3)}$, the local arrangement $T^{(3)}Be^{-T^{(1)}}Si^{-T^{(3)}}Si$ is forced by the bond-valence requirements of the T(1) tetrahedron. Hence ^{T(3)}Be cannot exceed ^{T(3)}Si in the substitution ^{T(4)}Si + ^{T(3)}Be + ^{O(2)}OH⁻ $\Rightarrow T^{(4)}A1 + T^{(3)}Si + O^{(2)}O^{2-}$, accounting for a range in substitution from Ca₄Be₂Si₇O₂₄(OH)₂ $[Si_2Al_2O_2]$ to $Ca_4Be_2Si_7O_{24}(OH)_2$ [BeAlSi₂(OH)O] (Beus, 1966) and the lack of

compositions between $Ca_4Be_2Si_7O_{24}(OH)_2$ [B e A l S i ₂ (O H) O] a n d $Ca_4Be_2Si_7O_{24}(OH)_2[Be_2Si_2(OH)_2].$

The role of Na in promoting 'excess' Be in the structure of bavenite

Inspection of Table 3 and Fig. 8 shows that Be does exceed 3.0 a.p.f.u. in bavenite, in apparent contradiction to the above argument that Be \rightleftharpoons Si substitution is limited by local bond-valence requirements at the T(1) tetrahedron. However,



FIG. 15. The linkage of two T(3)-T(4)-T(3)-T(4) rings along the **c** direction through the T(1) tetrahedron projected onto (100); in the upper part of the figure, the *Ca* site is occupied by Ca (blue), whereas in the lower part of the figure, the *Ca* site is occupied by Na (yellow). Note that H(2) forms a hydrogen bond with O(1) where locally associated with Na at the *Ca* site, and the adjacent T(3) site is occupied by Be, forming a T(3)Be-T(1)Si-T(3)Be link.

Fig. 9 shows that this 'excess' Be is accompanied by replacement of Ca by Na. This is a rather unusual substitution as both substituents (Na, Be) must replace cations of higher formal charge. In order to maintain electroneutrality, either there must be replacement of Si by Al by the amount (Na + excess Be) or replacement of O by (OH). The above argument that incorporation of Be at T(3) must be accompanied by incorporation of (OH) at O(2) still holds, and hence the substitution is thus

$$\stackrel{T(3)}{\Longrightarrow} Be + \stackrel{O(2)}{\longrightarrow} OH^- + Na + \stackrel{T(4)}{\longrightarrow} Si_2$$

$$\stackrel{T(3)}{\Longrightarrow} Si + \stackrel{O(2)}{\longrightarrow} O^{2-} + Ca + \stackrel{T(4)}{\longrightarrow} Al_2.$$

Although the amounts involved are small, this substitution is also indicated by the fact that the two Be-rich (and Na-rich) points in Fig. 5 (corresponding to 12BAV and 35BAV) lie below the 1:1 line between $^{T(4)}Al$ and $^{T(3)}Be$. This second substitution is similar to the first, with the addition of Na + $^{T(4)}Si \rightleftharpoons Ca + ^{T(4)}Al$; as none of these constituents is Be, one needs to ask (1) what is the role of Na in this substitution, and (2) how does the incorporation of Na negate the linkage constraint (in the **c** direction) on the amount of Be in the structure?

Figure 15 shows the local arrangement around the T(3)-T(1)-T(3) linkage in the **c** direction. The upper H(2) hydrogen shows the usual hydrogenbond to the O(3) anion where T(3) is occupied by Be. In Fig. 15, the T(3) tetrahedron (top right, labelled Be) links to a T(1) tetrahedron (labelled Si) as shown (horizontally) in Fig. 14. This T(1)tetrahedron then links (shown in Fig. 15) to a T(3)tetrahedron of another T(3) - T(4) - T(3) - T(4)ring, and the lower T(3) tetrahedron is commonly constrained to be occupied by Si (as discussed above). However, if the Ca site is actually occupied by Na (Fig. 15, bottom), the adjacent H(2) is not as strongly repelled from Na as from Ca, and can form a hydrogen bond with the adjacent O(1) anion as shown at the bottom of Fig. 15. This arrangement will provide more bond valence to O(1) which is normally the case where the Ca site is occupied by Ca. Is it enough to materially effect the occupancy of the adjacent T(3) site? As discussed above, the bond-valence incident at the linking T(1) tetrahedron is $0.44 \times$ $2 [T(2) - O(9) \times 2] + 0.27 \times 4 [Ca - O(9) \times 4] +$ $0.41 \times 1 [T(3) - O(1), T(3) = Be] + 0.21 \times$ $4 [Ca-O(1) \times 4] + X [T(3)-O(1), T(3) = not$ specified] = (3.21 + X) v.u. where X is the bond valence supplied by the other T(3) site involved in the T(3)-T(1)-T(3) linkage in the **c** direction. For the local arrangement where the Ca site is occupied by Na (Fig. 15, top), this value of (3.21 + X) v.u. is modified by subtracting the value for one Ca-O(1) bond (0.21 v.u., Table 8a), replacing it by the bond valence from the analogous Na-O(1) bond (0.18 v.u.), and adding the contribution from the hydrogen bond (0.27 v.u., Table 8a), leading to a bond-valence incident at the linking T(1) tetrahedron of (3.21 - 0.21 + 0.18)



FIG. 16. The FTIR spectrum for Na-bearing bavenite BAV35 in the principal OH-stretching region; data are shown as hollow squares.

(+0.27 + X) = 3.45 v.u.: X = 0.55 v.u. This value is significantly closer to the short-range Be-O(1)value of 0.41 v.u. than the corresponding Si-O(1)value of 0.81 v.u. (Table 8*a*,*b*), indicating that Be can occupy the second T(3) tetrahedron in the T(3)-T(1)-T(3) linkage in the **c** direction where the adjacent Ca site is occupied by Na instead of Ca. The difference between the Be-O(1) values of 0.41 and 0.55 v.u., and the close approach of the H(2) and Na atoms probably make this a highly strained arrangement, but it is clear from the compositions observed for 12BAV and 35BAV that this arrangement can occur in small amounts. However, such strain obviously limits the amount of this substitution, accounting for the rarity of bayenite compositions with Be >3 a.p.f.u.

The change in hydrogen bonding in the Nabearing structure is visible in the IR. Figure 16 shows the IR spectrum of bavenite 35BAV with 0.145 Na a.p.f.u. In addition to the five bands that are present in all the other bavenite spectra recorded (Fig. 12), there is a band at ~3590 cm⁻¹ that is not present in the other spectra. We assign this to the proposed H(2)...O(1) hydrogen bond associated with the incorporation of Na into the bavenite structure.

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